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THE UNIVERSITY OF IOWA  
Department of Mechanical Engineering

Fracture Mechanics  
ME:5159

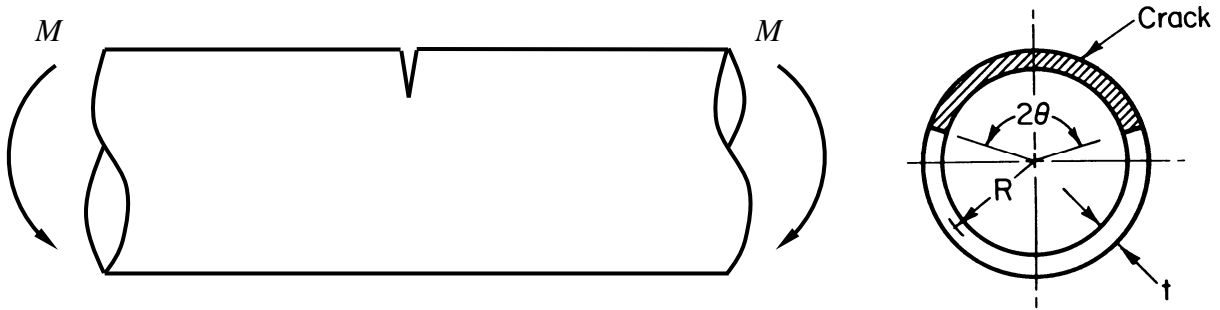
Homework #5  
Total Points: 20

Assigned: April 13, 2020  
Due: April 20, 2020

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**Problem 1:**

Consider a pipe with a circumferential through-wall crack that is subjected to pure bending, as shown in the figure below.



The pipe has outer diameter  $D_o = 457.2$  mm, wall thickness  $t = 21.77$  mm, and initial crack size  $\theta_0/\pi = 0.2$ . The material is Type 304 stainless steel and has the stress-strain curve and  $J$ - $R$  curve which can be conveniently modeled by Ramberg-Osgood and power-law equations:

$$\frac{\varepsilon}{\varepsilon_0} = \frac{\sigma}{\sigma_0} + \alpha \left( \frac{\sigma}{\sigma_0} \right)^n \quad \text{and}$$

$$J_R = J_{Ic} + C (\Delta a)^m,$$

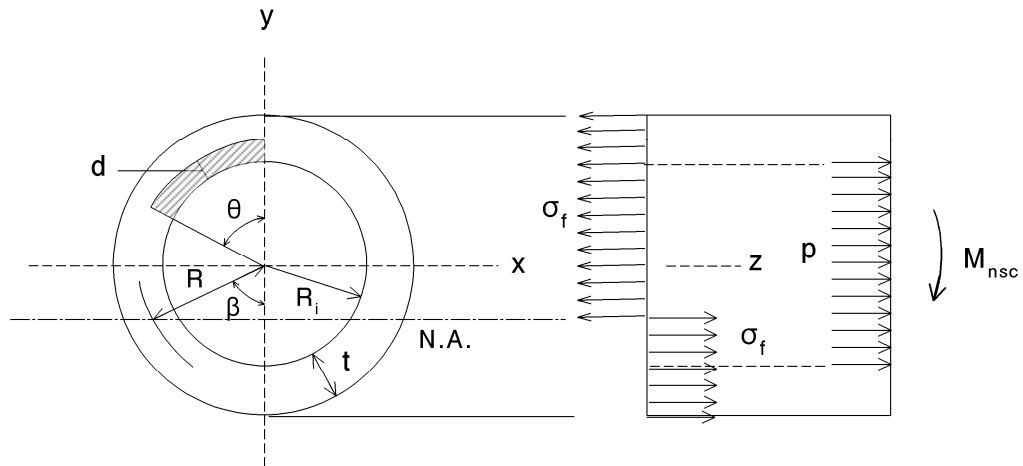
respectively, where  $E = 182.7$  GPa,  $\sigma_0 = 155$  MPa,  $\alpha = 8.1$ ,  $n = 3.8$ ,  $J_{Ic} = 0.5$  MJ/m<sup>2</sup>,  $C = 3.5$ , and  $m = 0.5$ . Also,  $S_y = 155$  MPa and  $S_u = 443$  MPa.

Using the GE/EPRI EPFM method and the closed-form  $F(\theta/\pi, R/t)$  and  $h_1(\theta/\pi, n, R/t)$  functions (see *Engineering Fracture Mechanics* paper, Vol. 52, No. 2, 1995), calculate (1) the initiation moment  $M_i$  and (2) the maximum moment  $M_{max}$  for this cracked pipe. Assuming that the flow stress  $\sigma_f$  is the average of yield and ultimate strengths calculate also (3) the net-section-collapse moment  $M_{nsc}$  for this pipe.

**Problem 2:**

Consider a pipe with a circumferential, constant-depth, internal part-through surface crack of total angle  $2\theta$  and depth  $d$ , as shown in the figure (note: the crack is symmetrical about y-axis and only half of crack is shown). The pipe and crack geometry parameters are defined in the figure. The pipe is subjected to combined bending and longitudinal tension,  $P = \pi R_i^2 p$  with  $p$  representing the internal pipe pressure. If  $\sigma_f$  is the flow stress of the material, show that the net-section-collapse moment  $M_{nsc}$  is:

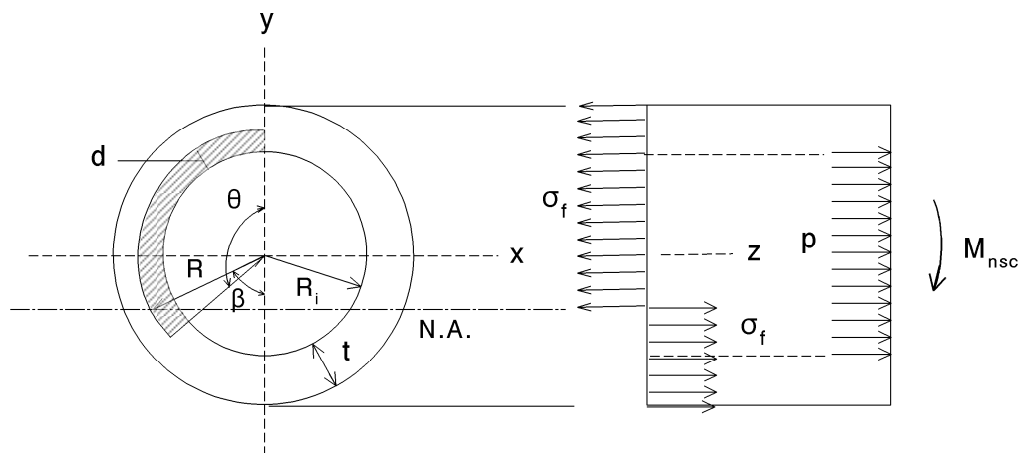
(a) For  $\theta < \pi - \beta$  (Entire Crack in Tension Zone).



$$M_{nsc} = 2R^2 t \sigma_f \left[ 2 \sin \beta - \frac{d}{t} \sin \theta \right]$$

$$\beta = \frac{\pi - \theta(d/t)}{2} - \frac{\pi R_i^2 p}{4R \sigma_f t}$$

(b) For  $\theta \geq \pi - \beta$  (Part of Crack in Compression Zone).



$$M_{nsc} = 2R^2 t \sigma_f \left[ 2 - \frac{d}{t} \right] \sin \beta$$

$$\beta = \frac{\pi}{2 - (d/t)} \left[ 1 - (d/t) - \frac{R_i^2 p}{2R \sigma_f t} \right]$$