

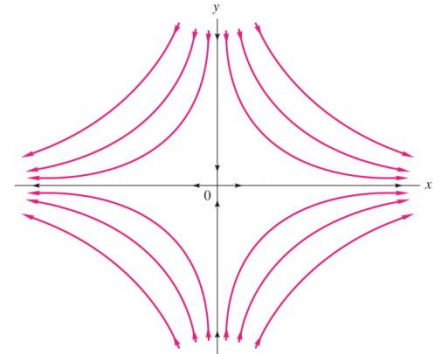
NAME _____

Fluids-ID _____

Quiz 4. The velocity field near a stagnation point (see figure) may be written in the form

$$u = \frac{U_0 x}{L} \quad v = -\frac{U_0 y}{L}$$

where U_0 and L are constants. For the particular case $L = 1.5$ m, if the resultant acceleration at $(x, y) = (1 \text{ m}, 1 \text{ m})$ is 25 m/s^2 , what is the value of U_0 ?



- For two-dimensional flow:

$$a_x = \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y}$$

$$a_y = \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y}$$

Solution:

For two-dimensional flow, the acceleration components are

$$a_x = \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} = 0 + \left(\frac{U_0 x}{L}\right) \left(\frac{U_0}{L}\right) + \left(-\frac{U_0 y}{L}\right) (0) = \frac{U_0^2}{L^2} x \quad (+4 \text{ points})$$

and

$$a_y = \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} = 0 + \left(\frac{U_0 x}{L}\right) (0) + \left(-\frac{U_0 y}{L}\right) \left(-\frac{U_0}{L}\right) = \frac{U_0^2}{L^2} y \quad (+4 \text{ points})$$

For the given resultant acceleration of 25 m/s^2 at $(x, y) = (1 \text{ m}, 1 \text{ m})$,

$$|a| = 25 \frac{\text{m}}{\text{s}^2} = \sqrt{a_x^2 + a_y^2} = \frac{U_0^2}{L^2} \sqrt{x^2 + y^2} = \frac{U_0^2}{(1.5 \text{ m})^2} \sqrt{2} \text{ m}$$

Solve for U_0 ,

$$U_0 = 6.3 \frac{\text{m}}{\text{s}} \quad (+2 \text{ points})$$