3.98

3.98 A conical plug is used to regulate the air flow from the pipe shown in Fig. P3.98. The air leaves the edge of the cone with a uniform thickness of 0.02 m. If viscous effects are negligible and the flowrate is 0.50 m³/s, determine the pressure within the pipe.

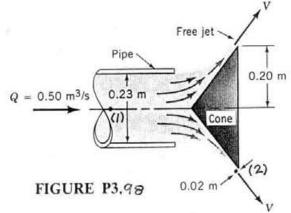


FIGURE P3.98 0.02 m

$$\frac{\rho_{1}}{\delta} + \frac{V_{1}^{2}}{2g} + Z_{1} = \frac{\rho_{2}}{\delta'} + \frac{V_{2}^{2}}{2g} + Z_{2} \quad \text{where } Z_{1} = Z_{2} \text{ and } \rho_{2} = 0$$
Also,
$$V_{1} = \frac{Q}{A_{1}} = \frac{0.5 \frac{m^{3}}{s}}{\frac{\pi}{4} (0.23m)^{2}} = 12.0 \frac{m}{s}$$
and
$$V_{2} = \frac{Q}{A_{2}} = \frac{Q}{2\pi Rh} = \frac{0.5 \frac{m^{3}}{s}}{2\pi (0.2m)(0.02m)} = 19.9 \frac{m}{s}$$
Thus,
$$\rho_{1} = \frac{1}{2} \rho \left(V_{2}^{2} - V_{1}^{2} \right) = \frac{1}{2} \left(1.23 \frac{kg}{m^{3}} \right) \left(19.9^{2} - 12.0^{2} \right) \frac{m^{2}}{s^{2}} = 15.5 \frac{N}{m^{2}}$$