

5.132

5.132 Water flows steadily in a pipe and exits as a free jet through an end cap that contains a filter as shown in Fig. P5.132. The flow is in a horizontal plane. The axial component, R_y , of the anchoring force needed to keep the end cap stationary is 60 lb. Determine the head loss for the flow through the end cap.

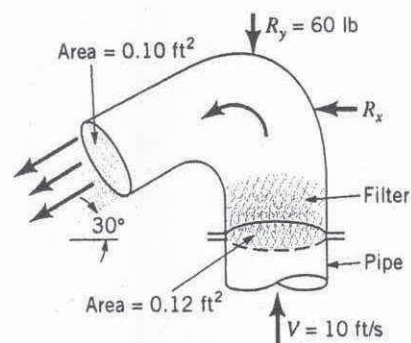


FIGURE P5.132

The y -component of the momentum equation, $\int_{cs} \rho \vec{V} \cdot \hat{n} dA = \sum F_y$, for the control volume shown is

$$(1) \quad V_1 \rho (-V_1) A_1 + (-V_2 \sin 30^\circ) \rho V_2 A_2 = p_1 A_1 - R_y$$

where $V_1 = 10 \text{ ft/s}$ and

$$V_2 = \frac{A_1}{A_2} V_1 = \left(\frac{0.12 \text{ ft}^2}{0.10 \text{ ft}^2} \right) (10 \text{ ft/s}) = 12 \text{ ft/s}$$

Thus, since $\rho A_1 V_1 = \rho A_2 V_2$, Eq. (1) gives

$$\begin{aligned} p_1 A_1 &= R_y - \rho V_1^2 A_1 - \rho V_2^2 \sin 30^\circ A_2 = R_y - \rho A_1 V_1 [V_1 + V_2 \sin 30^\circ] \\ &= 60 \text{ lb} - (1.94 \frac{\text{slug}}{\text{ft}^3}) (0.12 \text{ ft}^2) (10 \frac{\text{ft}}{\text{s}}) [10 \frac{\text{ft}}{\text{s}} + 12 \frac{\text{ft}}{\text{s}} \sin 30^\circ] = 22.8 \text{ lb} \end{aligned}$$

Hence,

$$p_1 = 22.8 \text{ lb} / A_1 = 22.8 \text{ lb} / (0.12 \text{ ft}^2) = 190 \text{ lb/ft}^2$$

From the energy equation for this flow,

$$\frac{p_1}{\rho} + \frac{V_1^2}{2g} - h_L = \frac{V_2^2}{2g}, \text{ or}$$

$$h_L = \frac{p_1}{\rho} + \frac{V_1^2 - V_2^2}{2g} = \frac{190 \text{ lb/ft}^2}{62.4 \text{ lb/ft}^3} + \frac{(10 \text{ ft/s})^2 - (12 \text{ ft/s})^2}{2 (32.2 \text{ ft/s}^2)} = \underline{\underline{2.36 \text{ ft}}}$$

