

2.143

2.143 A 1-m-diameter cylindrical mass, M , is connected to a 2-m-wide rectangular gate as shown in Fig. P2.143. The gate is to open when the water level, h , drops below 2.5 m. Determine the required value for M . Neglect friction at the gate hinge and the pulley.

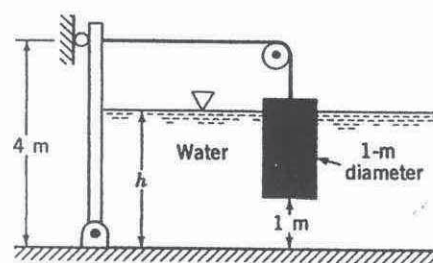


FIGURE P2.143

$$F_R = \gamma h_c A$$

$$= \gamma \left(\frac{h}{2} \right) h (2)$$

$$= \gamma h^2$$

where all lengths are in m.

For equilibrium,

$$\sum M_O = 0$$

so that

$$4T = \left(\frac{h}{3} \right) F_R = \gamma \frac{h^3}{3}$$

and

$$T = \frac{\gamma h^3}{12}$$

For the cylindrical mass $\sum F_{\text{vertical}} = 0$ and

$$T = Mg - F_B = Mg - \gamma V_{\text{mass}}$$

Thus,

$$M = \frac{T + \gamma V_{\text{mass}}}{g} = \frac{\frac{\gamma h^3}{12} + \gamma \left(\frac{\pi}{4} \right) (1)^2 (h - 1)}{g}$$

and for $h = 2.5 \text{ m}$

$$M = \frac{(9.80 \times 10^3 \frac{\text{N}}{\text{m}^3}) \left[\frac{(2.5 \text{ m})^3}{12} + \frac{\pi}{4} (1 \text{ m})^2 (2.5 \text{ m} - 1.0 \text{ m}) \right]}{9.81 \frac{\text{m}}{\text{s}^2}}$$

$$= \underline{\underline{2480 \text{ kg}}}$$

