

9.54

9.54 A 38.1-mm-diameter, 0.0245-N table tennis ball is released from the bottom of a swimming pool. With what velocity does it rise to the surface? Assume it has reached its terminal

For steady rise $\Sigma F_z = 0$ or $F_B = W + \mathcal{D}$, where $\mathcal{D} = drag = C_D \frac{1}{2} \rho U^2 \# D^2$ W = weight = 0.0245 N

 $F_B = b_{UOyant} \text{ force } = \delta \forall = \delta \frac{4\pi}{3} \left(\frac{D}{2}\right)^3$

Thus, $S = \frac{4\pi}{3} \left(\frac{D}{2}\right)^{3} = W + C_{D} + \frac{1}{2} \rho U^{2} + \frac{\pi}{4} D^{2}$ or $\left(9.80 \times 10^{3} \frac{N}{m^{3}}\right) + \frac{4\pi}{3} \left(\frac{0.0381}{2}\right)^{3} = 0.0245 N + \frac{1}{2} C_{D} \left(999 + \frac{kq}{m^{3}}\right) U^{2} + \frac{\pi}{4} (0.0381 m)^{3}$

1 U dia. D = 38.1mm

water

or $C_D U^2 = 0.455, \text{ where } U \sim \frac{m}{s} \tag{1}$

Also, $Re = \frac{UD}{V}$

 $Re = \frac{U(0.0381m)}{1.12 \times 10^{-6} \frac{m^2}{s}} = 3.40 \times 10^4 U, \text{ where } U = \frac{m}{s}$ (2)

Finally, from Fig. 9.21: CD

Trial and error solution: Assume CD; obtain U from Eq.(1), Re from Eq.(2); check CD from Eq.(3), the graph.

Assume $C_D = 0.5 \longrightarrow U = 0.954 \frac{m}{s} \longrightarrow Re = 3.24 \times 10^4 \longrightarrow C_D = 0.4 \neq 0.5$ Assume $C_D = 0.4 \longrightarrow U = 1.06 \frac{m}{s} \longrightarrow Re = 3.62 \times 10^4 \longrightarrow C_D = 0.4 \text{ (checks)}$ Thus, $U = 1.06 \frac{m}{s}$

Note: Because of the graph (Fig. 9.21) the answers are not accurate to three significant figures.