

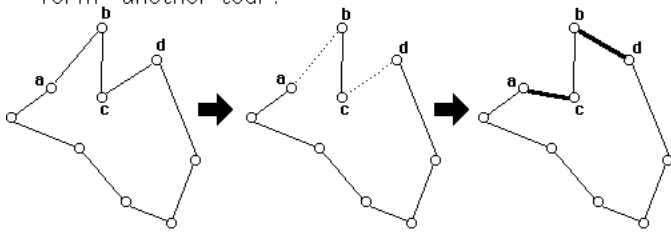
Exchange Algorithm for the Traveling Salesman Problem

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Exchange heuristics, given an initial tour, try to replace k edges of the tour with k edges not on the tour in order to find a shorter tour.

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A k -exchange is performed by deleting k edges of a tour, and reconnecting the segments so as to form another tour.



Example: a 2-exchange

Edges **ab** and **cd** are replaced by **ac** and **bd**

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For a specified integer k , a k -neighborhood of a tour is one which might be obtained by a k -exchange.

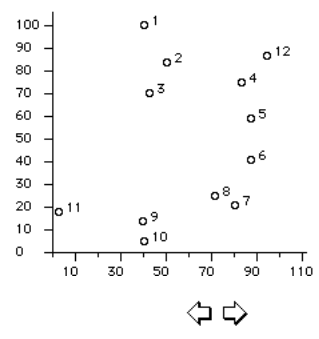
If no shorter tour exists in a k -neighborhood of a tour, that tour is said to be k -optimal.

(Only if a tour is k -optimal for every $k \leq N/2$ can we be certain that the tour is truly optimal!)

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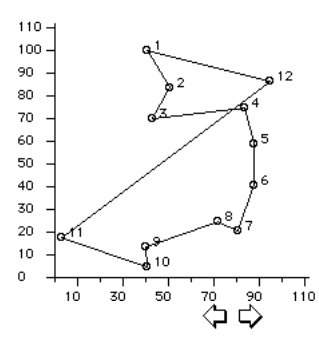
Example

Random Symmetric TSP
(seed= 133398)



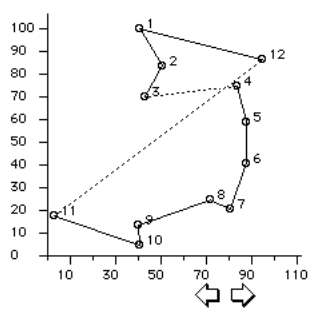
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Lin's 2-exchange heuristic



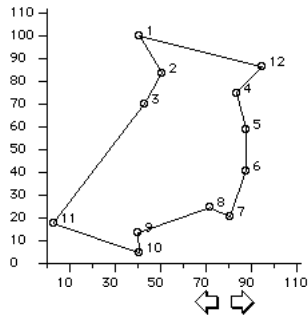
*Initial tour
(found by
nearest
neighbor
heuristic)*

Tour # 1 is 1 2 3 / 11 10 9 8 7 6 5 4 / 12 1
 Length: 321 Improvement: 74



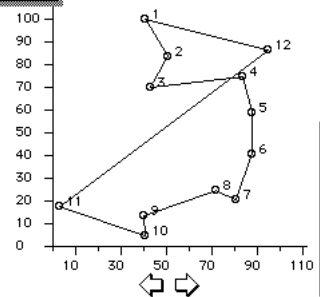
Edges (3,4) & (11,12) are removed, breaking tour into 2 paths. These can then be reconnected in only one other way.

2-Optimal Tour: 1 2 3 11 10 9 8 7 6 5 4 12 1,
with length 321



No 2-neighbor
tour gives any
improvement

3-exchange
heuristic

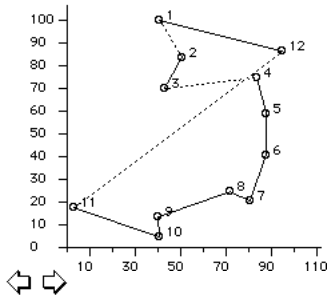


Initial tour
(found by
nearest
neighbor
heuristic)

Exchange type: 1
Replace edges: 1 3 11, i.e., (1 2), (3 4), & (11 12)
having length 175
with edges (1 2), (3 11), & (4 12) having length 101
Tour # 1 is 1 2 3 11 10 9 8 7 6 5 4 12 1 with length: 321
Improvement: 74

Because edge (1,2) was
re-inserted, this is
actually a 2-neighbor
tour!

3-exchange
heuristic



3-Optimal Tour: 1 2 3 11 10 9 8 7 6 5 4 12 1,
with length 321

No further
improvement
was found.

