

The "Nearest Insertion" heuristic constructs a tour for the TSP as follows:

- step 0: Select an initial node i. Let N' denote the set of nodes N - { i } Let T = { (i, i) }
- step 1: Let $\hat{j} = \underset{j \in N'}{\operatorname{argmin}} \left[\underset{i \in T}{\min} \left\{ d_{ij} \right\} \right]$
- step 2: Let (i',i") = argmin $\{d_{i_1j} + d_{ji_2} d_{i_1i_2}\}$ $(i_1,i_2) \in T$

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The "Nearest Insertion" heuristic algorithm constructs a tour, starting with an arbitrary node.

Each step begins with a subtour, and selects the node which is *nearest* to the set of nodes on the subtour to be added to the subtour. After selecting the node k to be added, an edge (i,j) is selected and the edges (i,k) and (k,j)then replace the edge (i,j).

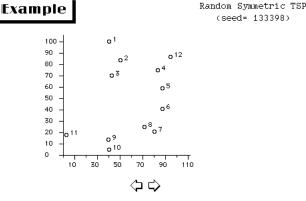
The edge (i,j) is selected so as to minimize the increase in the length of the subtour, i.e.,

$$d_{ik} + d_{kj} - d_{ij}$$

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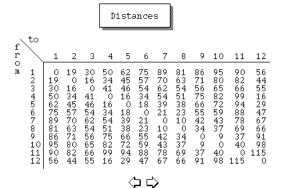
- $\begin{array}{l} \text{step 3: Replace arc}(i_1\,,i_2\,)\,\,\text{in the tour T with} \\ \text{the pair of arcs}\,\,(i_1\,,\hat{j}\,)\,\,\text{and}\,\,(\,\hat{j}\,,i_2\,). \\ \text{Let}\,\,\,\text{N'}=\text{N'}=\{\,\hat{j}\,\,\}\,\,\,\text{and}\,\,\,\hat{i}=\hat{j}. \end{array}$
- step 4: If $N' = \emptyset$, STOP. Else return to step 1.

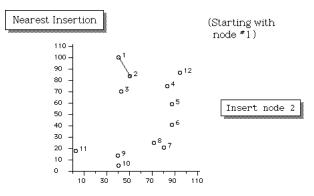
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Let's arbitrarily begin the tour with node #1, i.e., $T = \{1\}$, and N' = $\{2,3,4,5,6,7,8,9,10,11,12\}$

The nearest node to T={1} is node 2.

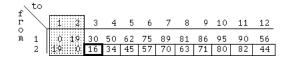




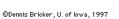
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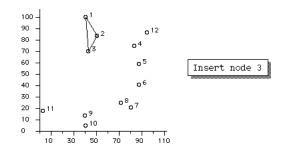
f r 0 M

The nearest node to the subtour $T = \{1,2\}$ is node #3.



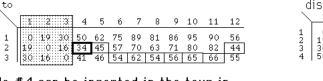
The nearest node to $T = \{1, 2, 3\}$ is node #4.





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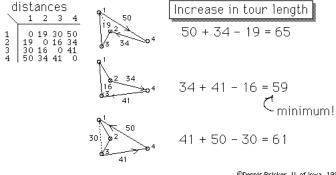
We insert node #4 in such a way as to minimize the increase in tour length:



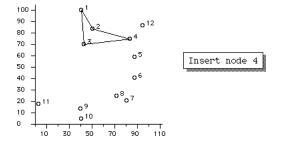
Node #4 can be inserted in the tour in 3 different ways: $1 \rightarrow 4 \rightarrow 2$

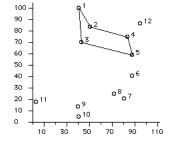
2	\rightarrow	4—	→3
3	\rightarrow	4—	→ 1

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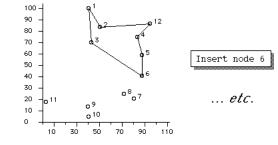
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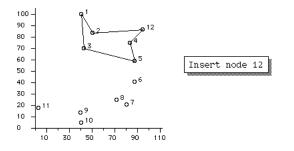


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Insert node 5

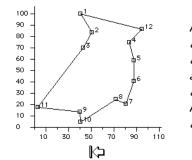


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Nearest Insertion Tour: 6 7 8 10 9 11 3 2 1 12 4 5 6, with length 321

> Note that the final tour varies according to the initial node in the tour!

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