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ALGORITHM

Given: a network with designated source & sink, each arc having a capacity in each direction. (Capacity of arc (i,j) need not equal that of (j,i))

Step 0 Initially, let the flow in each arc be zero.

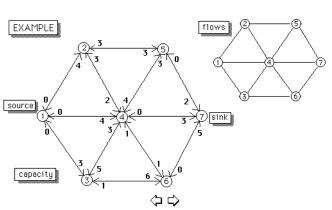
Step 1 Find any path from source to sink that has positive flow capacity (in direction of flow) for every arc in the path. If no such path exists, STOP.

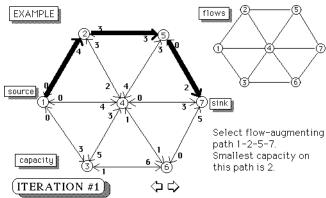
with positive capacity.)

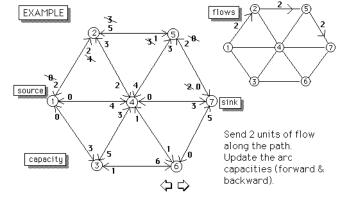
Step 2 Find the smallest arc capacity **k** on this path *(the flow-augmenting path).* Increase the flow in this path by **k**.

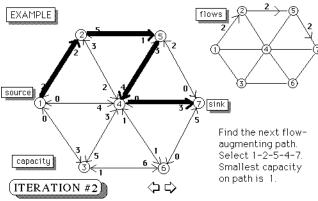
Step 3 For each arc in the flow-augmenting path, reduce all capacities in the direction of the flow by the amount **k**, and increase all capacities in the direction opposite the flow by **k**.

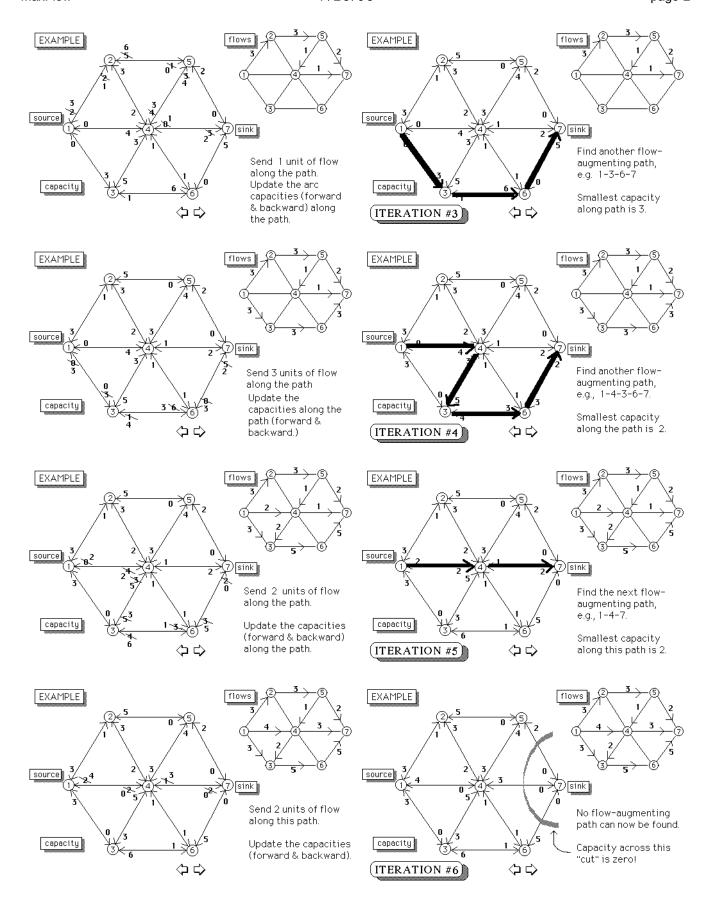
Return to Step 1.









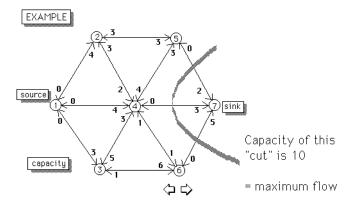


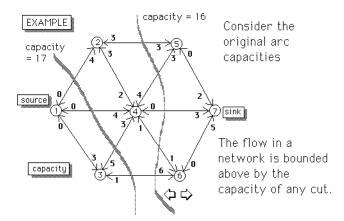
Definition

A $\mbox{\it cut}$ of a network is a partition of the node set N into 2 subsets, N_1 and N_2 , such that

- $N = N_1 \cup N_2$,
- $N_1 \cap N_2 = \emptyset$,
- the source node is in N_1 ,
- the sink node is in N₂

The *capacity* of the cut is $\sum_{i \in N_1} \sum_{j \in N_2} c_{ij}$





MAX-FLOW/MIN-CUT THEOREM

The maximum flow in a network is equal to the capacity of the cut having the minimum cut capacity.

