Markov Decision Processes			 A Markov Decision Process (MDP) is a classification of stochastic Dynamic Programming models. An MDP consists of a finite set <i>S</i> of states and, for each state <i>s</i> ∈ <i>S</i>, a finite set <i>A_s</i> of alternative actions. When in state <i>s</i> at stage n and action a∈ A_s is selected, a reward r(s,a) is earned or a cost c(s,a) is incurred. The system then makes a transition into another state <i>s</i>' with probability <i>p^a_{s,s'}</i> ≡ <i>P</i>{<i>X_{n+1}</i> = <i>s</i>' <i>X_n</i> = <i>s</i> & action <i>a</i> ∈ <i>A_s</i> is selected}. 		
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Notes: • we assume s given state/a same for all s • the "Markov µ of the process the action sel • MDPs may ha many stages.	tationary transition probabiliti action combination i & j, the va stages. property" is assumed, that is, is is dependent <i>only</i> upon the lected), and not on any prior h ave either a finite number of s	es! That is, for a alue of p _{ij} is the the future behavior current state (and istory. stages or infinitely	Examples Maintenance pla Inventory replen No-claim limits f	nning ishment or auto insurance	
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Objective criterion • Finite numbe • Total exp • Total exp • Infinitely ma • Average • total exp	 Objective criterion Finite number N of stages: Total expected cost or return Total expected discounted cost or return Infinitely many stages: Average cost per stage (assuming steady state behavior) total expected discounted cost or return 		 Finite horizon MDPs may be solved by stochastic dynamic programming (DP). Infinite horizon MDPs may be solved by Value iteration (limit of DP solution as N→∞) Policy improvement algorithm Linear programming algorithm 		
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