

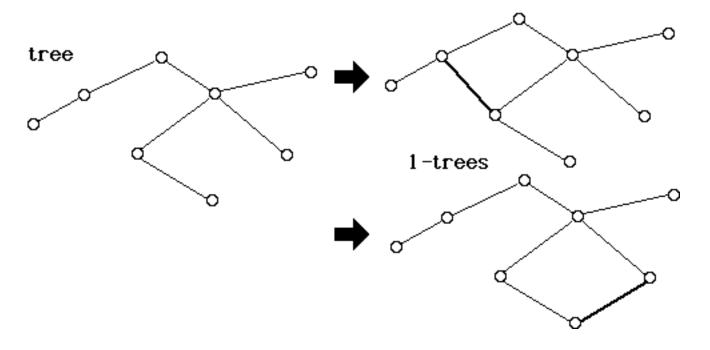
A TSP tour has the properties:

- it is a connected subgraph of the network
- the degree of every node is 2

The solution of the *Assignment Problem* satisfies the second property, but not always the first. The solution of the *minimum spanning 1-tree* problem satisfies the first property, but not always the second.

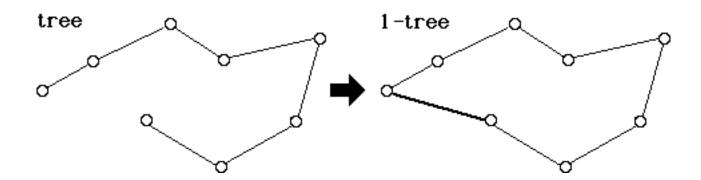
1-Tree

A 1-tree is constructed by adding a single edge to a tree.



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Note that a tour is a 1-tree:



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$$\label{eq:minimize} \begin{array}{ll} \text{Minimize} \sum\limits_{i=1}^{n} \sum\limits_{j=1}^{n} d_{ij} X_{ij} \\ \text{subject to} \\ & \sum\limits_{i=1}^{n} X_{ij} = 1 \ \forall \ j{=}1, \dots n \\ & \sum\limits_{j=1}^{n} X_{ij} = 1 \ \forall \ i{=}1, \dots n \end{array} \right) \begin{array}{l} \text{Assignment} \\ \text{constraints} \\ \text{constraints} \\ & X \in \textbf{T} \qquad \textit{= set of all 1-trees} \end{array}$$

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If either the assignment or the 1-tree constraints are relaxed, the resulting problem (which is easy to solve) provides a lower bound on the length of the optimal tour.



Relaxation of 1-tree constraints



Relaxation of Assignment constraints