

Decision Trees

- a diagram for analyzing decisions under risk, i.e., when the probability distins of the possible "states of nature" are known
- appropriate for a sequence of decisions, each of which could lead to one of several uncertain outcomes

EXAMPLES

I® PROTRAC, Inc.

IS AIRLINE TICKET PURCHASE

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OILCO

INCORPORATING NEW INFORMATION

PROTRAC, Inc., must decide on one of three marketing & prod'n strategies for a new line of home & garden tractors:

A: agressive

B: basic

C: cautious

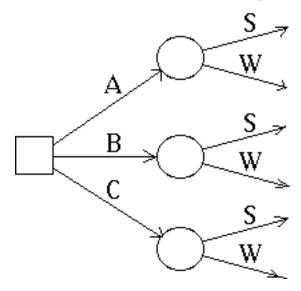
The condition of the market (as yet unknown) is categorized as "Strong" or "Weak", and determines the payoff:

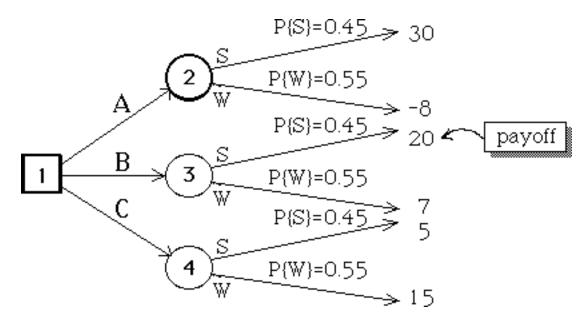


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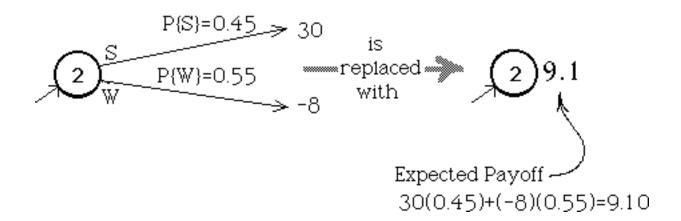
| | State of "Nature" | | |
|----------|-------------------|---------|-------------|
| | S: strong | W: weak | |
| Decision | 0.45 | 0.55 | Probability |
| A | 30 | -8 | |
| В | 20 | 7 | |
| С | 5 | 15 | |

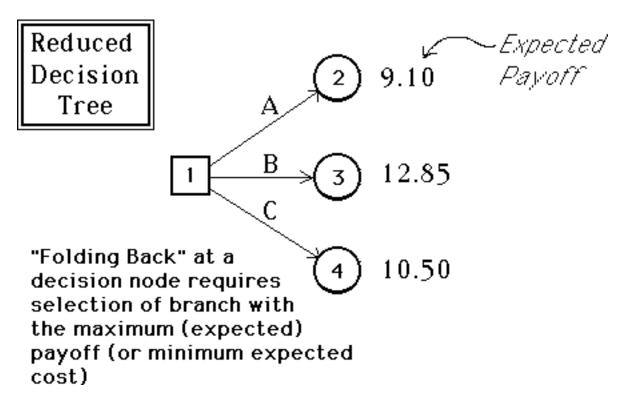
Represent the decision process as a "tree", with a SQUARE representing a decision, and a CIRCLE representing a random outcome:





"Folding Back" Terminal Branches of the Tree "Folding Back" at a random node requires computation of the expected payoff







When we "fold back" the tree at a decision node, the value of the node is the value of the optimal decision

1 12.85

Maximum Expected Payoff

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EXAMPLE

Erica is going to fly to London on August 5 and return home on August 20. It is now July 1.

On July 1, she may buy a one-way ticket (for \$350) or a round-trip ticket (for \$660).

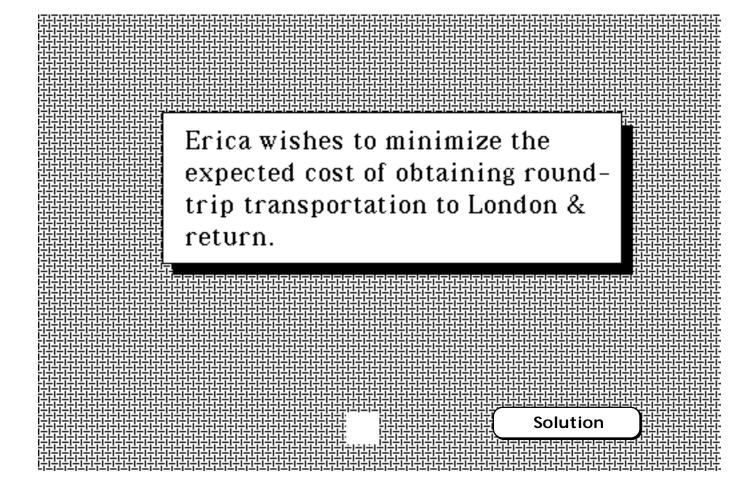
She may also wait until August 1 to buy a ticket.

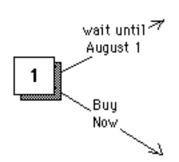
On August 1, a one-way ticket will cost \$370 and a round-trip ticket will cost \$730



It is possible (with probability 0.30) that between July 1 and August 1, her sister (who works for the airline) will be able to obtain a *free* one-way ticket for Frica.

If Erica has bought a round-trip ticket on July 1 and her sister has obtained a free ticket, she may return "half" of her round-trip ticket to the airline. In this case, her total cost will be \$330 plus a \$50 penalty.





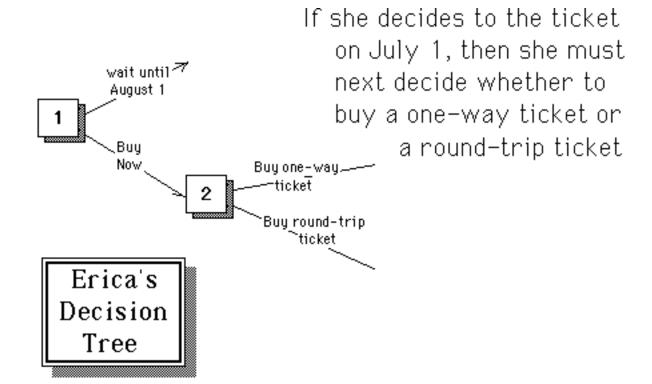
First, she must decide whether to

or

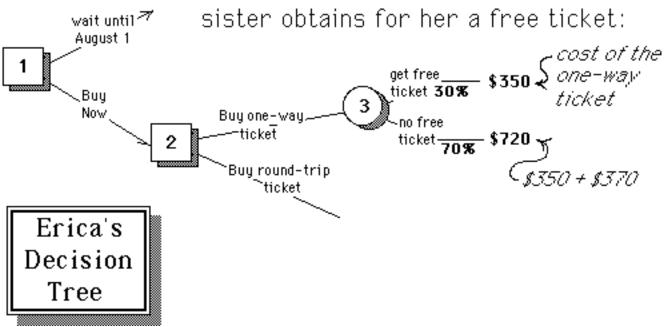
- buy a ticket now (July 1),
- wait until August 1

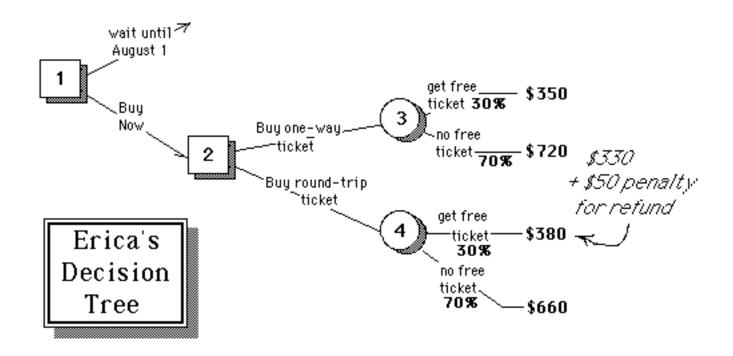
Erica's Decision Tree

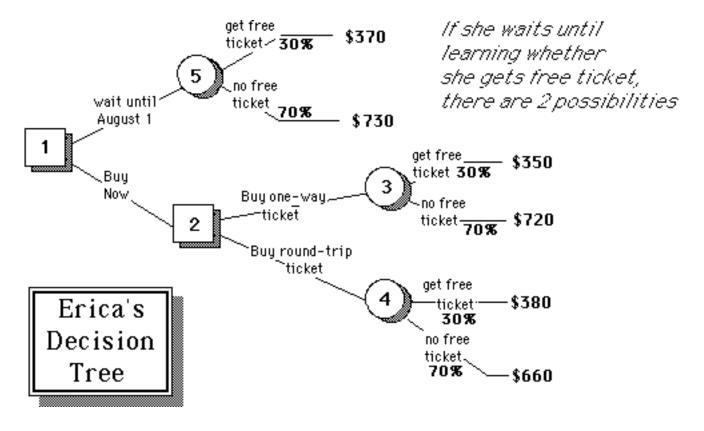


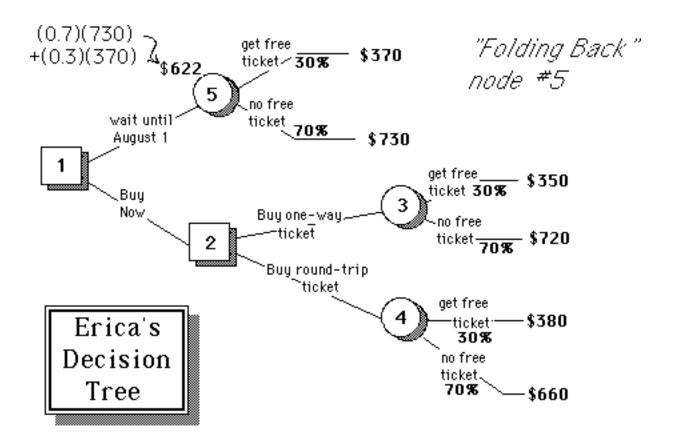


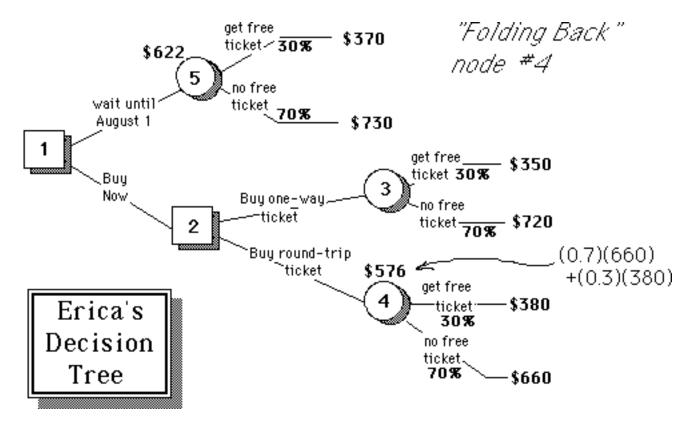
If she buys a one-way ticket, then her cost depends upon whether her sister obtains for her a free ticket:

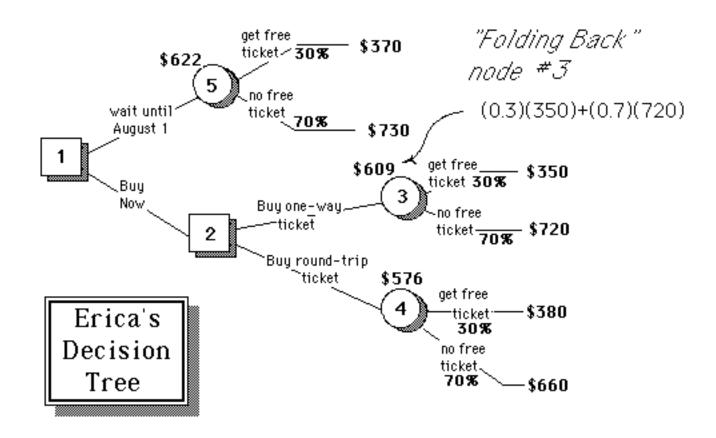


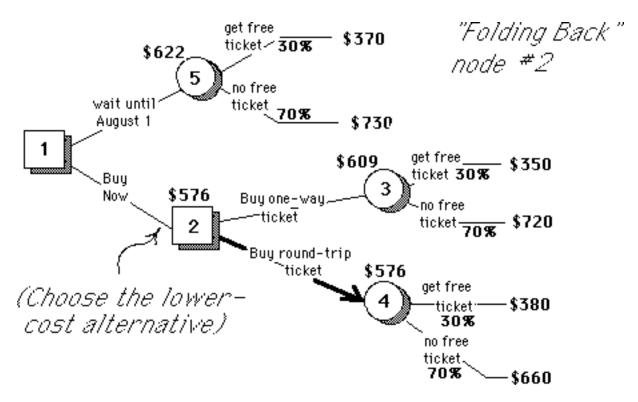


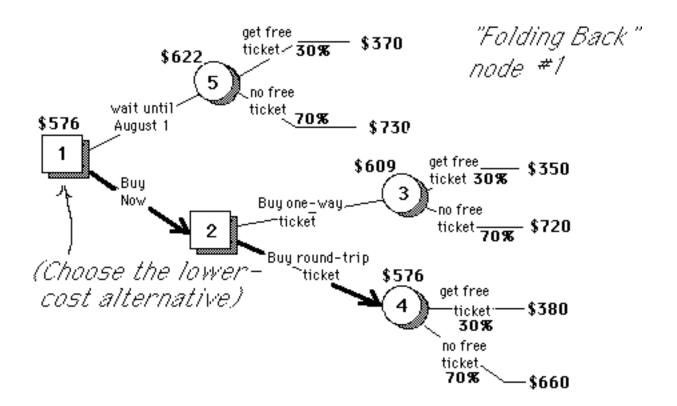












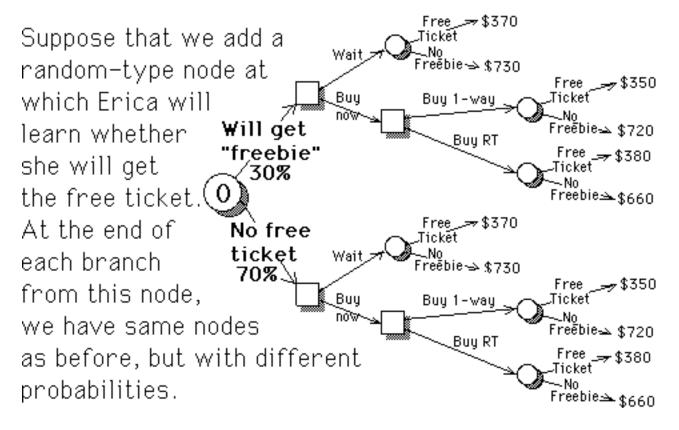
The optimal strategy is not to wait until August 1, but to buy a round-trip ticket now. Then, if she gets the free ticket, she should cancel half of the round-trip ticket which she purchased.

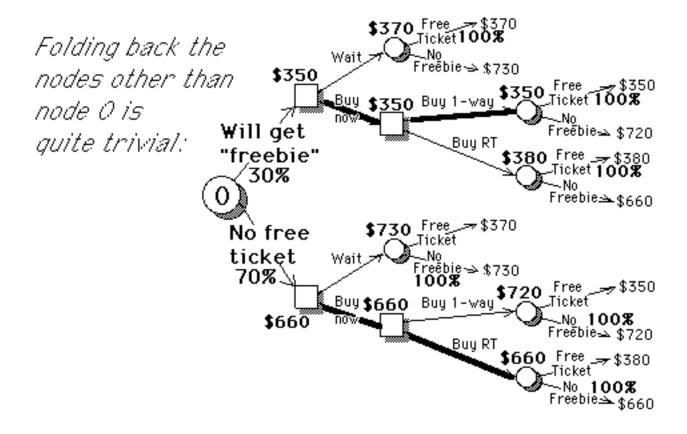
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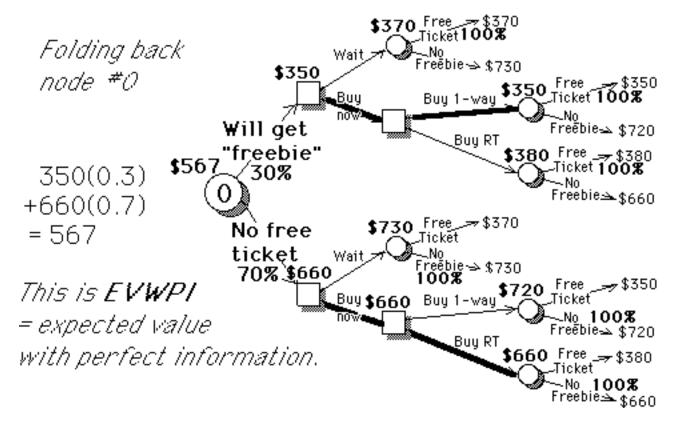
EVPI Expected **V**alue of **P**erfect **I**nformation

EVWOI = Expected Value Without Information = \$576 (cost)

What is EYWPI= Expected Value With Perfect Information?



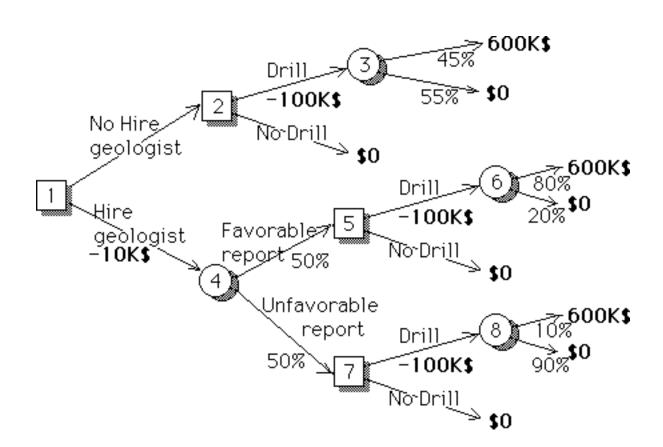




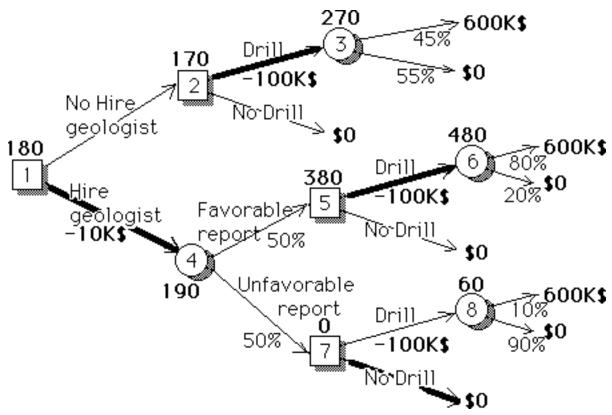
EVPI = EVWPI-EVWOI

If Erica had foreknowledge whether she would receive the free ticket, her expected cost would be reduced by \$9.

- Oilco must decide whether to drill for oil in the South China Sea.
- Cost of drilling is \$100,000.
- If oil is found, its value is estimated at \$600,000.
- Current estimate of P{oil} is 45%.
- Before drilling, the company can hire a geologist for \$10,000.
- There is 50% probability he will issue a favorable report, in which case P{oil} is 80%
- If unfavorable, P{oil} is 10%.



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Solution

Oilco should hire the geologist; if his report is favorable, they should drill, but if not favorable, they should not drill.

What is the expected value of

- sample information, i.e., the report of the geologist?
- perfect information?

