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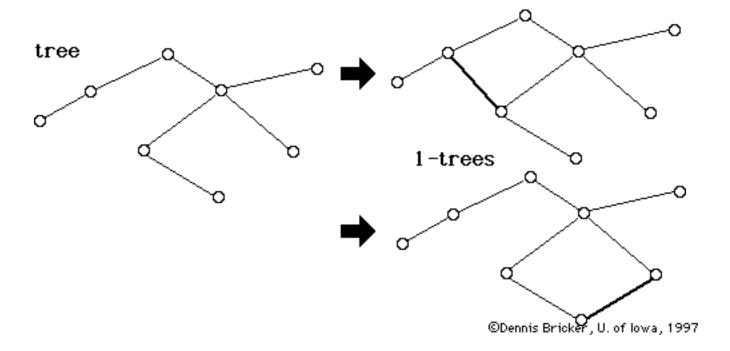
A TSP tour has the properties:

- it is a connected subgraph of the network
- the degree of every node is 2

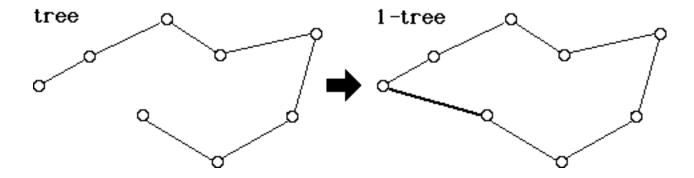
The solution of the *Assignment Problem* satisfies the second property, but not always the first. The solution of the *minimum spanning 1-tree* problem satisfies the first property, but not always the second.

1-Tree

A 1-tree is constructed by adding a single edge to a tree.



Note that a tour is a 1-tree:



$$\begin{aligned} & \text{Minimize} \sum_{i=1}^{n} \sum_{j=1}^{n} d_{ij} X_{ij} \\ & \text{subject to} \\ & \sum_{i=1}^{n} X_{ij} = 1 \ \forall \ j{=}1, \dots n \\ & \sum_{j=1}^{n} X_{ij} = 1 \ \forall \ i{=}1, \dots n \end{aligned} \end{aligned} \right. \underbrace{\begin{array}{c} \text{Assignment constraints} \\ \text{Constraints} \\ \text{Sign} \end{array}}_{\text{Sign}} X_{ij} = 1 \ \forall \ i{=}1, \dots n \end{aligned}$$

If either the assignment or the 1-tree constraints are relaxed, the resulting problem (which is easy to solve) provides a lower bound on the length of the optimal tour.



Relaxation of 1-tree constraints



Relaxation of Assignment constraints

