

**56:271 Nonlinear Programming**  
**Quiz #6 – Fall 2003**

1. **GRG** is an acronym meaning **G** \_\_\_\_\_ **R** \_\_\_\_\_ **G** \_\_\_\_\_ algorithm.
- |                |               |                |
|----------------|---------------|----------------|
| a. golden      | d. relative   | d. golden      |
| b. gradient    | b. removal    | b. gradient    |
| c. generalized | c. regression | c. generalized |
| d. Gaussian    | e. resource   | e. Gaussian    |
| e. geometric   | a. reduced    | a. geometric   |
| f. graphical   | f. rank       | f. graphical   |
- \_\_\_ 2. The function  $f(x,y) = xy$  is a ...
- |                       |                      |                    |
|-----------------------|----------------------|--------------------|
| a. concave function   | b. convex function   | c. linear function |
| d. separable function | e. none of the above |                    |

True (+) or false (o)?

- \_\_\_ 3. A function which is not convex is called "concave".
- \_\_\_ 4. The sum of two convex functions is convex.
- \_\_\_ 5. The product of two convex functions is convex.
- \_\_\_ 6. A linear function is both convex and concave.
- \_\_\_ 7. A positive definite matrix always has all positive elements, although a matrix whose elements are positive need not be positive definite.
- \_\_\_ 8. The "dependent" variables of the GRG algorithm are comparable to the "basic" variables of the LP simplex algorithm.
- \_\_\_ 9. In each iteration of the GRG algorithm, the values of several independent variables may be changed simultaneously.
- \_\_\_ 10. The GRG algorithm requires that dependent variables be at neither their upper nor lower bounds.
- \_\_\_ 11. A differentiable function is convex if and only if its Hessian matrix is non-negative.
- \_\_\_ 12. KKT are the initials of Karl K. Tucker, who developed necessary and sufficient conditions for constrained optimization.
- \_\_\_ 13. If constraints are linear, there is no need to re-partition the variables (dependent and independent) during the iterations of the GRG algorithm.
- \_\_\_ 14. The GRG algorithm uses a quadratic approximation of nonlinear objective functions.
- \_\_\_ 15. The GRG algorithm requires a dependent variable for each equality constraint.
- \_\_\_ 16. No line searches (i.e., one-dimensional searches) are used in the GRG algorithm.
- \_\_\_ 17. If GRG were applied to a linear programming problem, it would be identical to the simplex method.
- \_\_\_ 18. If  $g_i(x^0) = 0$  then  $x^0$  is feasible in the constraint  $g_i(x) \leq 0$  and at  $x^0$ ,  $\nabla g_i(x^0)$  is a direction pointing into the feasible region.
- \_\_\_ 19. If  $x^0$  is optimal in the problem "minimize  $f(x)$  s.t.  $g(x) \leq 0$ ", then the vectors  $\nabla f(x^0)$  and  $\nabla g(x^0)$  point in opposite directions.
- \_\_\_ 20. In each iteration of the GRG algorithm, the partition (into dependent & independent variables) is changed.