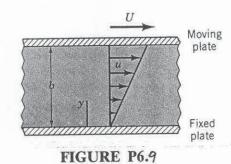
6. 9 An incompressible viscous fluid is placed between two large parallel plates as shown in Fig. P6.9. The bottom plate is fixed and the upper plate moves with a constant velocity, U. For these conditions the velocity distribution between the plates is linear, and can be expressed as

$$u = U \frac{y}{b}$$

Determine: (a) the volumetric dilatation rate, (b) the rotation vector, (c) the vorticity, and (d) the rate of angular deformation.



- (a) Volumetric dilatation rate =  $\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} = 0$
- (b) For velocity distribution given;  $\vec{\omega} = \omega_z \hat{k}$

and 
$$\omega_{2} = \frac{1}{2} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right) = -\frac{U}{2b}$$
Thus, 
$$\omega = -\frac{U}{2b} \frac{\lambda}{k}$$

(c) 
$$\overrightarrow{f} = 2\overrightarrow{\omega} = -\frac{\overrightarrow{U}}{b} + \hat{k}$$

$$(d) \quad \dot{\beta} = \frac{\partial v}{\partial x} + \frac{\partial u}{\partial y}$$

(Eg. 6.18)