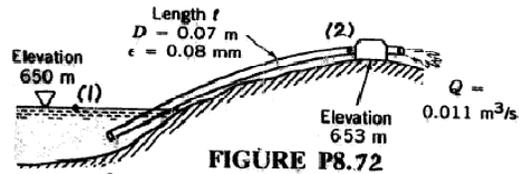


8.72 Water at 10 °C is pumped from a lake as shown in Fig. P8.72. If the flowrate is 0.011 m³/s, what is the maximum length inlet pipe, ℓ , that can be used without cavitation occurring?



$$\frac{p_1}{\rho} + \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\rho} + \frac{V_2^2}{2g} + z_2 + \left(f \frac{\ell}{D} + \sum K_L\right) \frac{V^2}{2g}, \text{ where } p_1 = 101 \text{ kPa}, z_1 = 650 \text{ m} \quad (1)$$

$V_1 = 0, V_2 = V, z_2 = 653 \text{ m}$, and from Table B.2 $p_2 = p_v = 1.228 \text{ kPa}$

$$\text{Also, } V = \frac{Q}{A} = \frac{0.011 \frac{\text{m}^3}{\text{s}}}{\frac{\pi}{4} (0.07 \text{ m})^2} = 2.86 \frac{\text{m}}{\text{s}} \text{ so that}$$

$$Re = \frac{VD}{\nu} = \frac{(2.86 \frac{\text{m}}{\text{s}})(0.07 \text{ m})}{1.307 \times 10^{-6} \frac{\text{m}^2}{\text{s}}} = 1.53 \times 10^5. \text{ With this } Re \text{ and from Table 8.1 with}$$

$$\frac{\epsilon}{D} = \frac{0.08 \text{ mm}}{70 \text{ mm}} = 0.00114 \text{ we obtain } f = 0.0216 \text{ (see Fig. 8.20)}$$

Hence, with $\sum K_L = 0.8$ for the entrance, Eq.(1) becomes

$$\frac{(101 - 1.228) \times 10^3 \frac{\text{N}}{\text{m}^2}}{9.80 \times 10^3 \frac{\text{N}}{\text{m}^2}} + 650 \text{ m} = 653 \text{ m} + \left(1 + (0.0216) \left(\frac{\ell}{0.07 \text{ m}}\right) + 0.8\right) \frac{(2.86 \frac{\text{m}}{\text{s}})^2}{2(9.81 \frac{\text{m}}{\text{s}^2})}$$

$$\text{or } \underline{\underline{\ell = 50.0 \text{ m}}}$$