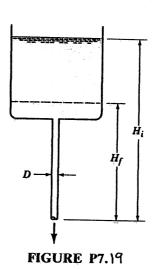
One type of viscometer consists of an open reservoir with a small diameter tube at the bottom as illustrated in Fig. P7.19. To measure viscosity the system is filled with the liquid of interest and the time required for the liquid level to fall from level H_i to H_f is determined. Use dimensional analysis to obtain a relationship between the viscosity, μ , and the draining time, τ . Assume that the other variables involved are the initial head, H_i , the final head, H_f , the tube diameter, D, and the specific weight of the liquid, y.



T=f(D, Hi, Hf, M, 8) T = T D = L $H_i = L$ $H_f = L$ $\mu = FL^{-2}T$ $\gamma = FL^{-3}$ From the pi theorem, 6-3=3 pi terms required. By inspection, for TT, (containing t):

$$T_{I} = \frac{T \times D}{\mu} = \frac{(T)(FL^{-3})(L)}{FL^{-2}T} = F^{\circ}L^{\circ}T^{\circ}$$

Check using MLT.

$$\frac{T*D}{\mu} \doteq \frac{(T)(ML^{-2}T^{-2})(L)}{ML^{-1}T^{-1}} \doteq M^{\circ}L^{\circ}T^{\circ} : ok$$
For TT_2 (containing H_i):

$$T_2 = \frac{H_L}{D}$$

 $TT_2 = \frac{Hc}{D}$ Which is obviously dimensionless. Similarly,

Thus,

$$\frac{\gamma \gamma D}{\mu} = \phi \left(\frac{H_c}{D}, \frac{H_f}{D} \right)$$

 $\frac{T8D}{\mu} = \phi \left(\frac{H_c}{D}, \frac{H_f}{D}\right)$ and for a fixed geometry (including H_c and H_c) $\frac{T8D}{\mu} = K$

$$\frac{T8D}{\mu} = K$$

Where K is a constant, depending on Hi/D and He/D.

From Eq. (1)

so that M = K, 87where $K_i = D/K$ and K_i is a constant for a fixed geometry.