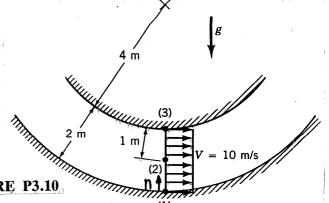
## 3.10

3.10 Water flows around the vertical two-dimensional bend with circular streamlines and constant velocity as shown in Fig. P3.10. If the pressure is 40 kPa at point (1), determine the pressures at points (2) and (3). Assume that the velocity profile is uniform as indicated.



$$-8\frac{dz}{dn} - \frac{\partial p}{\partial n} = \frac{\rho V^2}{R} \quad \text{with } \frac{dz}{dn} = 1 \quad \text{and} \quad V = 10 \, \text{m/s}$$

Thus, with 
$$R = 6 - n$$

$$\frac{d\rho}{dn} = -8 - \frac{\rho V^2}{6 - n} \quad \text{or} \quad$$

$$\int_{n=0}^{n} \frac{d\rho}{dn} dn = -\int_{n=0}^{\infty} 8dn - \int_{n=0}^{\infty} \frac{\rho V^2 dn}{6-n}$$

so that since 8 and Vare constants

$$\rho - \rho_1 = -\delta n - \rho V^2 \int_{n=0}^{\infty} \frac{dn}{\delta - n}$$

Thus

$$\rho = \rho_1 - 8n - \rho V^2 \ln \left( \frac{6}{6-n} \right)$$

With 
$$\rho_1 = 40 \text{ kPa}$$
 and  $n_2 = 1 \text{ m}$ :  $\rho_2 = 40 \text{ kPa} - 9.8 \times 10^3 \frac{N}{m^3} (1 \text{ m})$ 

$$-999 \frac{kg}{m^3} (10 \frac{m}{s})^2 \ln \left(\frac{6}{5}\right)$$

and

with 
$$\rho_1 = 40 \, k P_a$$
 and  $n_3 = 2m^3 \, \rho_3 = 40 \, k P_a - 9.80 \times 10^3 \, \frac{N}{m^3} (2m) - 999 \, \frac{kg}{m^3} (10 \, \frac{m}{s})^2 \, |n| (\frac{6}{4})$ 

or 
$$p_3 = -20.1 \, kPa$$