

# Chapter 8 Flow in Conduits

## Entrance and developed flows

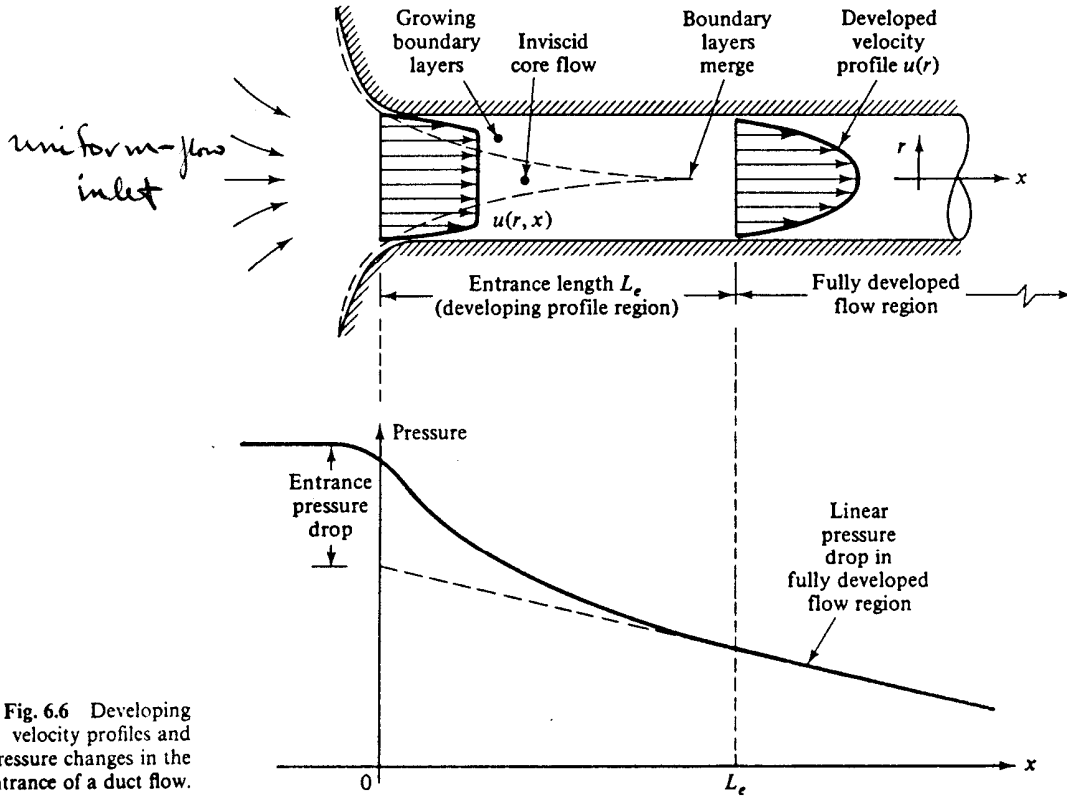


Fig. 6.6 Developing velocity profiles and pressure changes in the entrance of a duct flow.

$$L_e = f(D, V, \rho, \mu)$$

$$\Pi_i \text{ theorem} \Rightarrow L_e/D = f(Re)$$

Laminar flow:  $Re_{crit} \sim 2000$ , i.e., for  $Re < Re_{crit}$  laminar  
 $Re > Re_{crit}$  turbulent

$$L_e/D = .06Re \quad \text{from experiments}$$

$$L_{e_{max}} = .06Re_{crit}D \sim 138D$$

↙ maximum  $L_e$  for laminar flow

Turbulent flow:

$$\frac{Le}{D} \sim 4.4 Re^{1/6}$$

from experiment

| Re     | Le/D |
|--------|------|
| 4000   | 18   |
| $10^4$ | 20   |
| $10^5$ | 30   |
| $10^6$ | 44   |
| $10^7$ | 65   |
| $10^8$ | 95   |

i.e.,  
 relatively  
 shorter  
 than for  
 laminar  
 flow

Laminar vs. Turbulent Flow

*Hayson 1839  
 noted difference  
 in  $\Delta p = \Delta p(V)$   
 but could not  
 explain two  
 regimes*

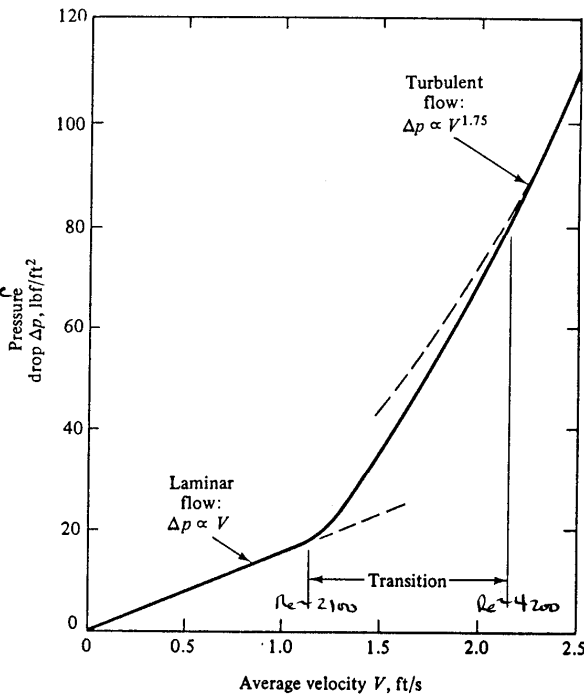
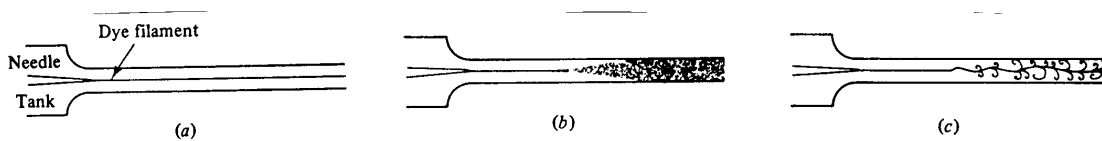


Fig. 6.4 Experimental evidence of transition for water flow in a 1/2-in smooth pipe 10 ft long.



laminar

turbulent

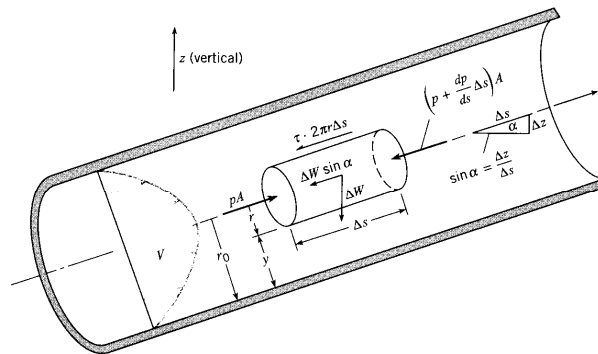
spark photo

Reynolds 1883 showed difference depends on  $Re = \frac{VD}{\nu}$

## Shear-Stress Distribution Across a Pipe Section

Continuity:  $Q_1 = Q_2 = \text{constant}$

FIGURE 10.1  
 Variation of shear stress  
 in a pipe.



i.e.,  $V_1 = V_2$  since  $A_1 = A_2$

Momentum: 
$$\begin{aligned} \sum F_s &= \sum \rho u (\underline{V} \cdot \underline{A}) \\ &= \rho V_1 (-V_1 A_1) - \rho V_2 (V_2 A_2) \\ &= \rho Q (V_2 - V_1) = 0 \end{aligned}$$

$$pA - \left( p + \frac{dp}{ds} ds \right) A - \Delta W \sin \alpha - \tau(2\pi r) ds = 0$$

$$\Delta W = \gamma A ds \quad \sin \alpha = \frac{dz}{ds}$$

$$-\frac{dp}{ds} ds A - \gamma A ds \frac{dz}{ds} - \tau(2\pi r) ds = 0$$

$$\div A ds \quad \tau = \frac{r}{2} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$\tau$  varies linearly from 0.0 at  $r = 0$  (centerline) to  $\tau_{\max}$  ( $= \tau_w$ ) at  $r = R$  (wall). Valid for laminar and turbulent flow.

## Laminar Flow in Pipes

$$\tau = \mu \frac{dV}{dy} = -\mu \frac{dV}{dr} = \frac{r}{2} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$$y = \text{wall coordinate} = r_o - r \Rightarrow \frac{dV}{dr} = \frac{dV}{dy} \frac{dy}{dr} = -\frac{dV}{dy}$$

$$\frac{dV}{dr} = -\frac{r}{2\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$$V = -\frac{r^2}{4\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right] + C$$

$$\underbrace{V(r_o)}_{\text{no slip condition}} = 0 \Rightarrow C = \frac{r_o^2}{4\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$$V(r) = \frac{r_o^2 - r^2}{4\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

Exact solution to  
 Navier-Stokes  
 equations for laminar  
 flow in circular pipe

$$Q = \int \underline{V} \cdot d\underline{A}$$

$$= \int_0^{r_o} V(r) \underbrace{2\pi r dr}$$

$$V_{\max} = \frac{r_o^2}{4\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

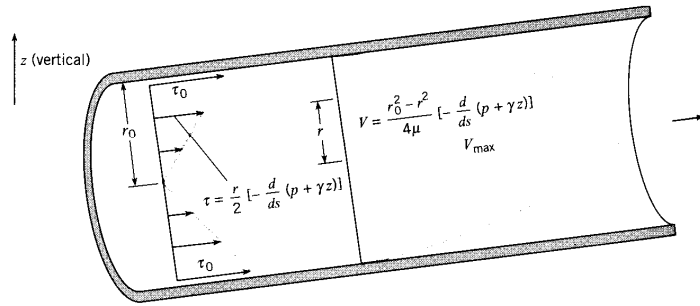
$$dA = r dr d\theta = r dr (2\pi)$$

$$Q = \frac{\pi r_o^4}{8\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$$\bar{V} = \frac{Q}{A} = \frac{r_o^2}{8\mu} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$$\bar{V} = \frac{V_{\max}}{2}$$

FIGURE 10.2  
 Distribution of shear stress and velocity for laminar flow in a pipe.



energy equation:

$$\frac{p_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + h_L$$

$$\Delta h = \left( \frac{p_2}{\gamma} + z_2 \right) - \left( \frac{p_1}{\gamma} + z_1 \right)$$

$$h_L = \frac{p_1 - p_2}{\gamma} + (z_1 - z_2) = -\Delta h$$

$$h_L = \frac{L}{\gamma} \left[ -\frac{d}{ds} (p + \gamma z) \right]$$

$L = \text{length of pipe} = ds$

$$= \frac{L}{\gamma} \left[ \frac{8\mu \bar{V}}{r_0^2} \right] = -\Delta h \alpha \bar{V}$$

$$h_L = L \left[ -\frac{d}{ds} \left( \frac{p}{\gamma} + z \right) \right]$$

$$= L \left( -\frac{dh}{ds} \right)$$

or  $h_f = h_L = \frac{32\mu L \bar{V}}{\gamma D^2}$

$h_f = \text{head loss due to friction}$

exact solution

$$\underbrace{\text{friction factor } f = \frac{8\tau_w}{\rho \bar{V}^2}}_{\text{friction coefficient for pipe flow}}$$

$$\underbrace{C_f = \frac{\tau_w}{\frac{1}{2}\rho V^2}}_{\text{boundary layer flow}}$$

$$\tau_w = \frac{r_o}{2} \left[ -\frac{d}{ds}(p + \gamma z) \right]$$

$$= \frac{r_o}{2} \left[ \frac{8\mu \bar{V}}{r_o^2} \right]$$

$$\tau_w = \frac{4\mu \bar{V}}{r_o}$$

$$f = \frac{32\mu}{\rho r_o \bar{V}} = \frac{64\mu}{\rho \bar{V} D} = \frac{64}{\text{Re}}$$

exact solution

$$\text{Re} = \frac{\bar{V} D}{\nu} \quad \nu = \frac{\mu}{\rho}$$

## Criterion for Laminar or Turbulent Flow in a Pipe

$Re_{crit} \sim 2000$       flow becomes unstable

$Re_{trans} \sim 3000$       flow becomes turbulent

$$Re = \bar{V}D/\nu$$

## Turbulent Flow in Pipes

Continuity and momentum:

$$\tau(r = r_o) = \tau_o = \frac{r_o}{2} \left[ -\frac{d}{ds}(p + \gamma z) \right]$$

$$\text{Energy: } h_f = \frac{L}{\gamma} \left[ -\frac{d}{ds}(p + \gamma z) \right]$$

$$\text{Combining: } h_f = \frac{L}{\gamma} \cdot \frac{2\tau_o}{r_o} \text{ define } f = \frac{\tau_o}{\frac{1}{8}\rho\bar{V}^2} = \text{friction factor}$$

$$h_f = \frac{L}{\rho g} \cdot \frac{2}{r_o} \cdot \frac{1}{8}\rho\bar{V}^2 f$$

$$h_f = f \cdot \frac{L}{D} \cdot \frac{\bar{V}^2}{2g} \quad \text{Darcy - Weisbach Equation}$$

$f = f(Re, k/D) = \text{still must be determined!}$

$$Re = \frac{\bar{V}D}{\nu} \quad k = \text{roughness}$$

## Velocity Distribution and Resistance in Smooth Pipes

As with turbulent boundary layers, mean-velocity follows three layer concept:

1. laminar sub-layer (viscous shear dominates)

$$u^+ = y^+ \quad 0 < y^+ < 5 \quad y^+ = \frac{yu^*}{\gamma} \quad y = r_o - r$$

$$u^* = \sqrt{\frac{\tau_o}{\rho}}$$

2. overlap layer (viscous and turbulent shear important)

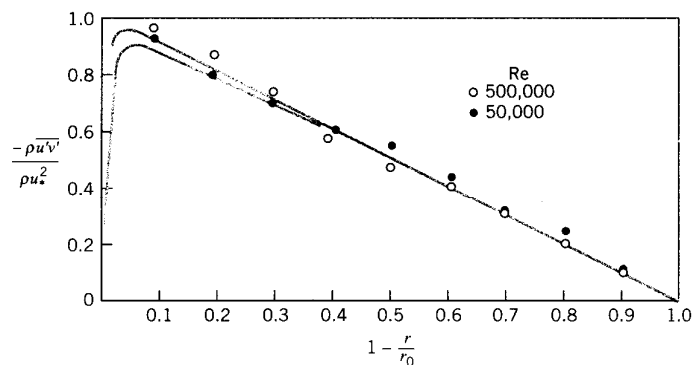
$$u^+ = \frac{1}{\kappa} \ln y^+ + B \quad 20 < y^+ < 10^5$$

$$\kappa = .41 \quad B = 5.5$$

3. outer layer (turbulent shear dominates)

$$\frac{U - u}{u^+} = f\left(1 - \frac{r}{r_o}\right) \quad y^+ > 10^5$$

FIGURE 10.4  
 Apparent shear stress in  
 a pipe. [After Laufer  
 (23)]





Assume log-law is valid across entire pipe

$$u^+ = \sqrt{\frac{\tau_w}{\rho}} = \text{friction velocity}$$

$$\frac{u(r)}{u^*} = \frac{1}{\kappa} \ln \frac{(r_o - r)u^*}{\nu} + B$$

$$\kappa = .41$$

$$B = 5.5$$

$$\bar{V} = \frac{Q}{A} = \frac{\int_0^{r_o} u(r) 2\pi r dr}{\pi r_o^2} = \frac{1}{2} u^* \left\{ \frac{2}{\kappa} \ln \frac{r_o u^*}{\nu} + 2B - \frac{3}{\kappa} \right\}$$

drop over bar: 
$$\frac{V}{u^*} = \underbrace{2.44 \ln \frac{r_o u^*}{\nu}}_{\frac{1}{2} \text{Re} \left( \frac{f}{8} \right)^{1/2}} + 1.34 = \left( \frac{\rho V^2}{\tau_o} \right)^{1/2} = \left( \frac{8}{f} \right)^{1/2}$$

$$\frac{1}{\sqrt{f}} = 1.99 \log(\text{Re } f^{1/2}) - 1.02$$

constants adjusted using data  $\Rightarrow \frac{1}{\sqrt{f}} = 2 \log(\text{Re } f^{1/2}) - .8 \quad \text{Re} > 3000$

Power law  $\Rightarrow f \sim .316 \text{Re}^{-1/4} \quad 4000 < \text{Re} < 10^5$

$$h_f = -\Delta h = -\left(\frac{\Delta p}{\gamma} + \Delta z\right) = f \frac{L}{D} \frac{V^2}{2g}$$

$$h_f = .316 \left(\frac{\mu}{\rho V D}\right)^{1/4} \frac{L}{D} \frac{V^2}{2g}$$

$$h_f \propto V^{1.75}$$

(recall  $h_f \propto V$  for laminar flow)

Other useful relationships

Power law fit to velocity profile:

$$\frac{u}{u_{\max}} = \left(\frac{y}{r_o}\right)^m \quad y = r_o - r$$

$$m = m(\text{Re})$$

$$\frac{u_{\max}}{u^*} = \frac{1}{\kappa} \ln \frac{r_o u^*}{r} + B$$

$$\frac{V}{u_{\max}} = \left(1 + 1.33f^{1/2}\right)^{-1}$$

TABLE 10.1 EXPONENTS FOR POWER-LAW EQUATION AND RATIO OF MEAN TO MAXIMUM VELOCITY

|                      |                           |                             |                             |                             |                             |
|----------------------|---------------------------|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| <b>Re</b> →          | <b>4 × 10<sup>3</sup></b> | <b>2.3 × 10<sup>4</sup></b> | <b>1.1 × 10<sup>5</sup></b> | <b>1.1 × 10<sup>6</sup></b> | <b>3.2 × 10<sup>6</sup></b> |
| <b>m</b> →           | $\frac{1}{6.0}$           | $\frac{1}{6.6}$             | $\frac{1}{7.0}$             | $\frac{1}{8.8}$             | $\frac{1}{10.0}$            |
| $\bar{V}/V_{\max}$ → | 0.791                     | 0.807                       | 0.817                       | 0.850                       | 0.865                       |

SOURCE: Schlichting (36). Used with permission of the McGraw-Hill Companies.

## Viscous Distribution and Resistance – Rough Pipes

For laminar flow, effect of roughness is small; however, for turbulent flow the effect is large. Both laminar sublayer and overlap layer are affected.

Inner layer:

$$u = u(y, k, \rho, \tau_w)$$

not function of  $\mu$  as was case  
for smooth pipe (or wall)

$$u^+ = u^+(y/k)$$

Outer layer: unaffected

Overlap layer:

$$u_R^+ = \frac{1}{\kappa} \ln \frac{y}{k} + \text{constant}$$

rough

$$u_S^+ = \frac{1}{\kappa} \ln y^+ + B$$

smooth

$$u_S^+ - u_R^+ = \underbrace{\frac{1}{\kappa} \ln k^+ + \text{constant}}_{\Delta B(k^+)}$$

$$k^+ = \frac{ku^*}{\nu}$$

i.e., rough-wall velocity profile shifts downward by  $\Delta B(k^+)$ , which increases with  $k^+$ .

three regions of flow depending on  $k^+$

1.  $k^+ < 5$       hydraulically smooth (no effect of roughness)
2.  $5 < k^+ < 70$       transitional roughness (Re dependence)
3.  $k^+ > 70$       fully rough (independent Re)

$$\begin{array}{l}
 \text{For 3, } \quad \Delta B = \frac{1}{\kappa} \ln k^+ - 3.5 \quad \text{from data} \\
 \\
 u^+ = \frac{1}{\kappa} \ln \frac{y}{k} + 8.5 \neq f(\text{Re}) \\
 \\
 \frac{V}{u^*} = 2.44 \ln \frac{D}{k} + 3.2 \\
 \\
 \frac{1}{f^{1/2}} = -2 \log \frac{k/D}{3.7}
 \end{array}
 \left. \vphantom{\begin{array}{l} \Delta B \\ u^+ \\ \frac{V}{u^*} \\ \frac{1}{f^{1/2}} \end{array}} \right\} \text{fully rough flow}$$

### Composite Log-Law

Smooth wall log law

$$u^+ = \frac{1}{\kappa} \ln y^+ + \underbrace{B - \Delta B(k^+)}_{B^*}$$

$$B^* = 5 - \frac{1}{\kappa} \ln(1 + .3k^+) \quad \text{from data}$$

$$\frac{1}{f^{1/2}} = -2 \log \left[ \frac{k/D}{3.7} + \frac{2.51}{\text{Re} f^{1/2}} \right] \quad \text{Moody Diagram}$$

$$= 1.14 - 2 \log \left( \frac{k_s}{D} + \frac{9.35}{\text{Re} f^{1/2}} \right)$$

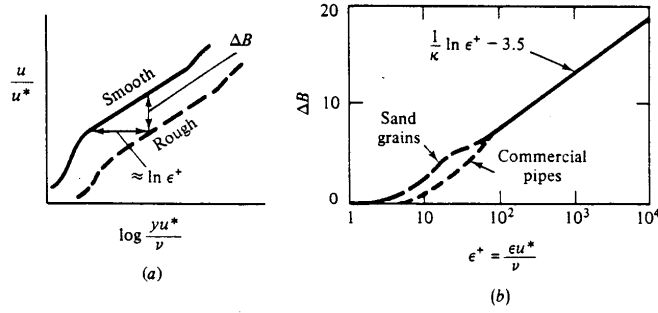


Fig. 6.12 Effect of wall roughness on turbulent pipe-flow velocity profiles: (a) logarithmic downshift; (b) correlation with roughness

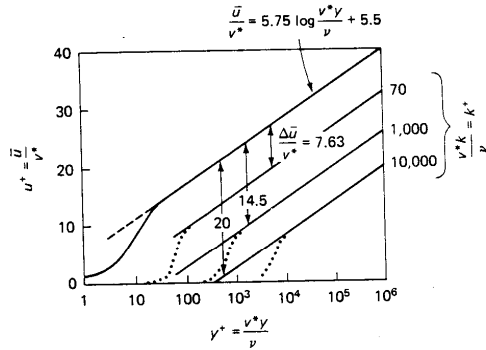


FIGURE 6-11 Experimental rough-pipe velocity profiles by Scholz (1955), showing the upward shift  $\Delta B$  of the logarithmic overlap layer.

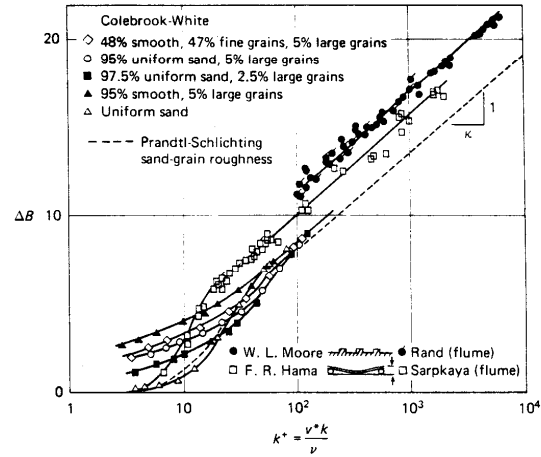


FIGURE 6-12 Composite plot of the profile-shift parameter  $\Delta B(k^+)$  for various roughness geometries, as compiled by Clauser (1956).

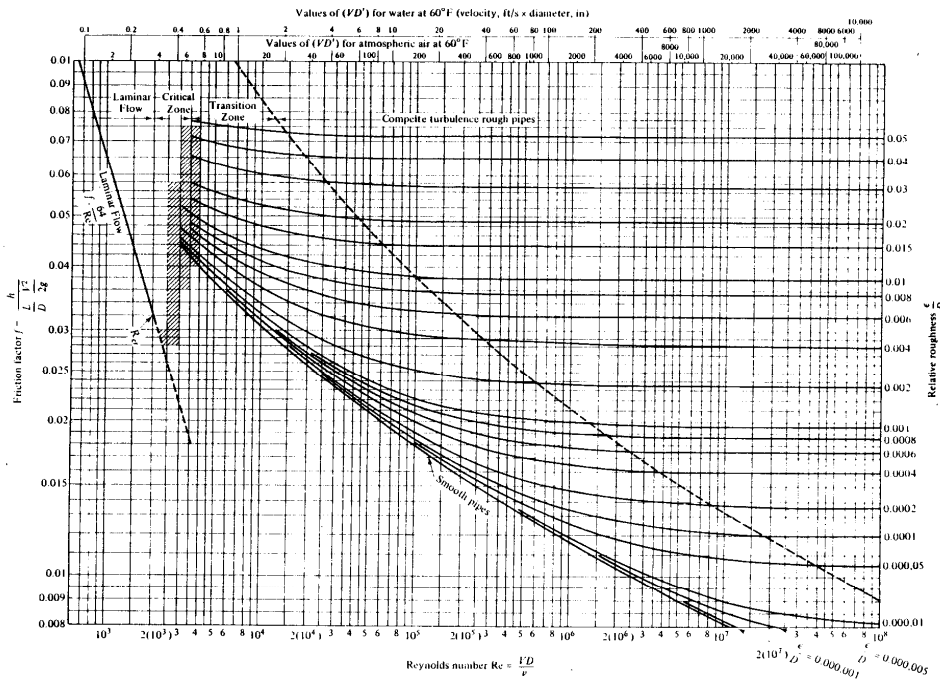


Fig. 6.13 The Moody chart for pipe friction with smooth and rough walls. (From Ref. 8, by permission of the ASME.)

FIGURE 10.7  
 Resistance coefficient  
 $f$  versus  $Re$  for sand-  
 roughened pipe. [After  
 Nikuradse (30)]

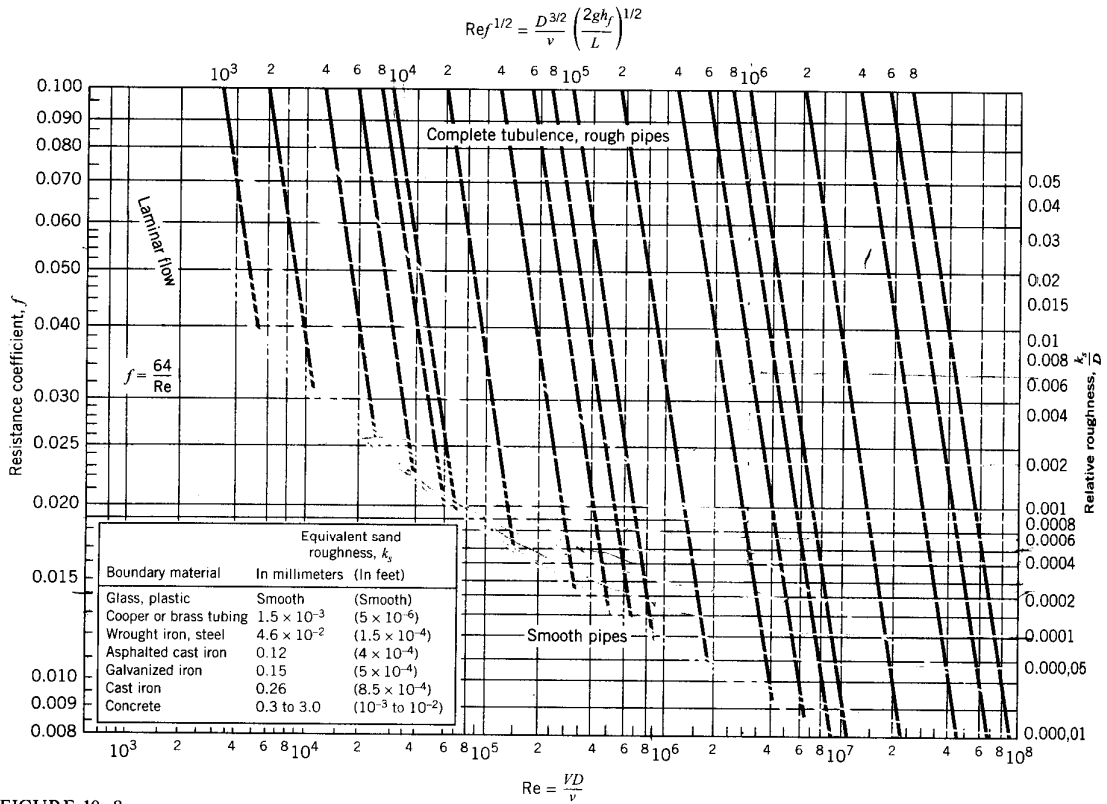
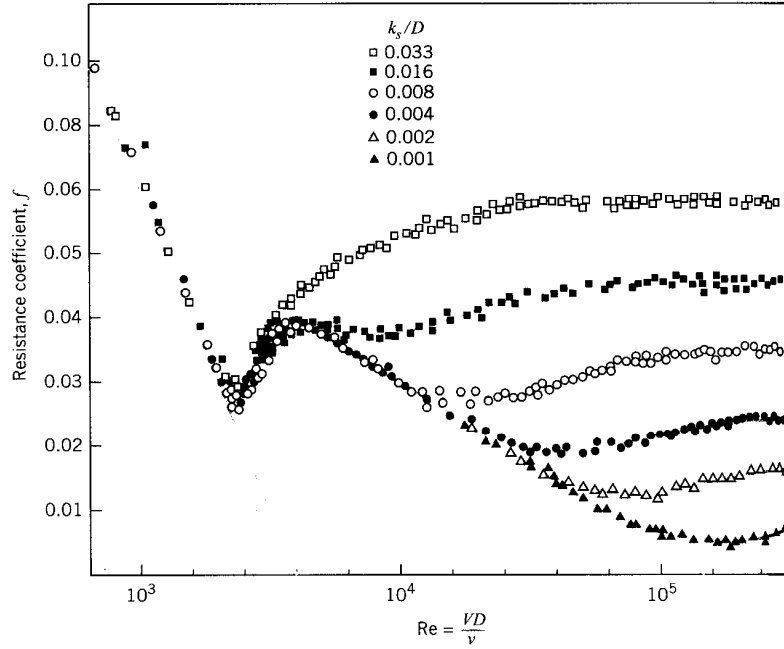
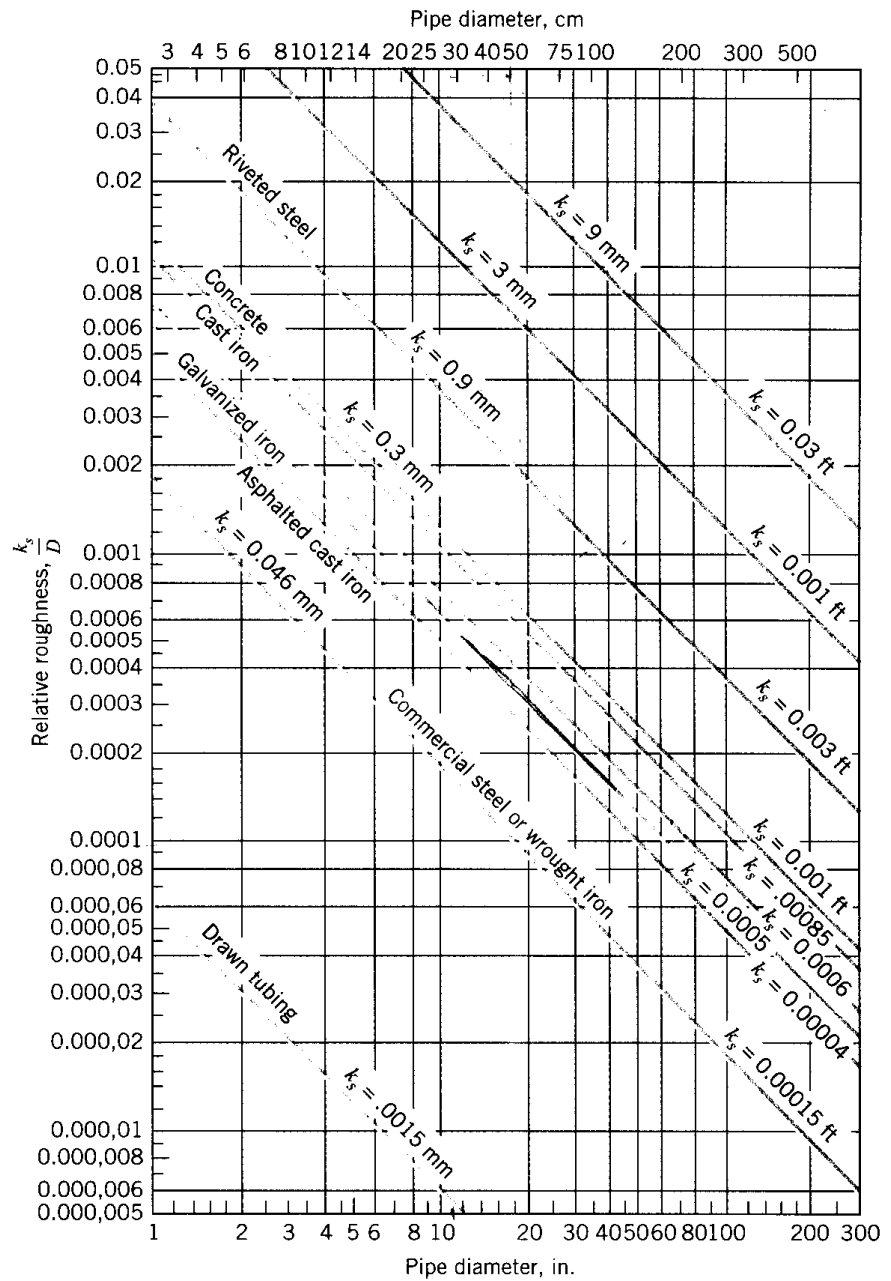


FIGURE 10.8  
 Resistance coefficient  $f$   
 versus  $Re$ . Reprinted  
 with minor variations.  
 [After Moody (29).  
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**FIGURE 10.9**  
*Relative roughness for various kinds of pipe.*  
 [After Moody (29).  
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There are basically three types of problems involved with uniform flow in a single pipe:

1. Determine the head loss, given the kind and size of pipe along with the flow rate,  $Q = A \cdot V$
2. Determine the flow rate, given the head, kind, and size of pipe
3. Determine the pipe diameter, given the type of pipe, head, and flow rate

1. Determine the head loss

The first problem of head loss is solved readily by obtaining  $f$  from the Moody diagram, using values of  $Re$  and  $k_s/D$  computed from the given data. The head loss  $h_f$  is then computed from the Darcy-Weisbach equation.

$$f = f(Re_d, k_s/D)$$

$$h_f = f \frac{L}{D} \frac{V^2}{2g} = -\Delta h \quad \Delta h = \left( \frac{p_2}{\gamma} + z_2 \right) - \left( \frac{p_1}{\gamma} + z_1 \right)$$

$$= -\Delta \left( \frac{p}{\gamma} + z \right)$$

$$Re_d = Re_d(V, D)$$

2. Determine the flow rate

The second problem of flow rate is solved by trial, using a successive approximation procedure. This is because both  $Re$  and  $f(Re)$  depend on the unknown velocity,  $V$ . The solution is as follows:



- 1) solve for  $V$  using an assumed value for  $f$  and the Darcy-Weisbach equation

$$V = \underbrace{\left[ \frac{2gh_f}{L/D} \right]^{1/2}}_{\text{known from given data}} \cdot f^{-1/2}$$

known from  
given data

note sign

- 2) using  $V$  compute  $Re$
- 3) obtain a new value for  $f = f(Re, k_s/D)$  and repeat as above until convergence

Or can use  $Re = f^{1/2} = \frac{D^{3/2}}{\nu} \left( \frac{2gh_f}{L} \right)^{1/2}$

scale on Moody Diagram

- 1) compute  $Re f^{1/2}$  and  $k_s/D$

- 2) read  $f$

- 3) solve  $V$  from  $h_f = f \frac{L}{D} \frac{V^2}{2g}$

- 4)  $Q = VA$

3. Determine the size of the pipe

The third problem of pipe size is solved by trial, using a successive approximation procedure. This is because  $h_f$ ,  $f$ , and  $Q$  all depend on the unknown diameter  $D$ . The solution procedure is as follows:

- 1) solve for D using an assumed value for f and the Darcy-Weisbach equation along with the definition of Q

$$D = \underbrace{\left[ \frac{8LQ^2}{\pi^2 gh_f} \right]^{1/5}}_{\text{known from given data}} \cdot f^{1/5}$$

known from  
given data

- 2) using D compute Re and  $k_s/D$
- 3) obtain a new value of  $f = f(\text{Re}, k_s/D)$  and repeat as above until convergence

## **8.5 Flows at Pipe Inlets and Losses From Fittings**

For real pipe systems in addition to friction head loss these are additional so called minor losses due to

1. entrance and exit effects
  2. expansions and contractions
  3. bends, elbows, tees, and other fittings
  4. valves (open or partially closed)
- } can be large effect

For such complex geometries we must rely on experimental data to obtain a loss coefficient

$$K = \frac{h_m}{\frac{V^2}{2g}} \leftarrow \text{head loss due to minor losses}$$

In general,

$$K = K(\text{geometry, Re, } \varepsilon/D)$$

dependence usually  
not known

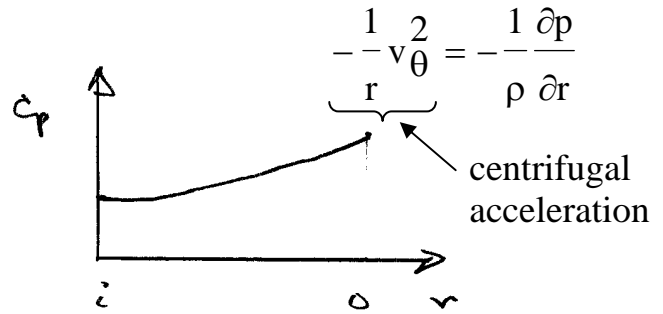
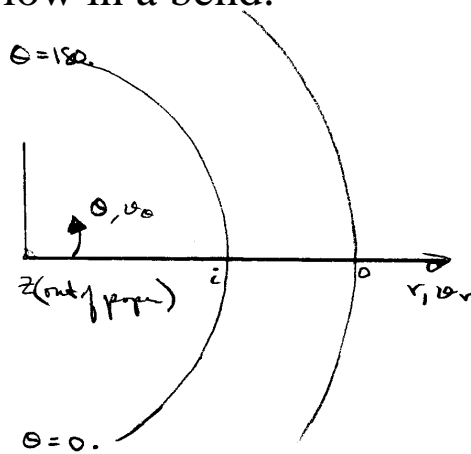
Loss coefficient data is supplied by manufacturers and also listed in handbooks. The data are for turbulent flow conditions but seldom given in terms of Re.

Modified Energy Equation to Include Minor Losses:

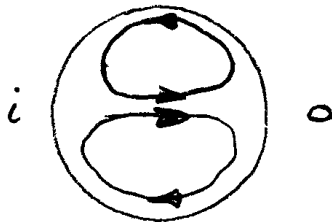
$$\frac{p_1}{\gamma} + z_1 + \frac{1}{2g} \alpha_1 V_1^2 + h_p = \frac{p_2}{\gamma} + z_2 + \frac{1}{2g} \alpha_2 V_2^2 + h_t + h_f + \sum h_m$$
$$h_m = K \frac{V^2}{2g}$$

Note:  $\sum h_m$  does not include pipe friction and e.g. in elbows and tees, this must be added to  $h_f$ .

### 1. Flow in a bend:

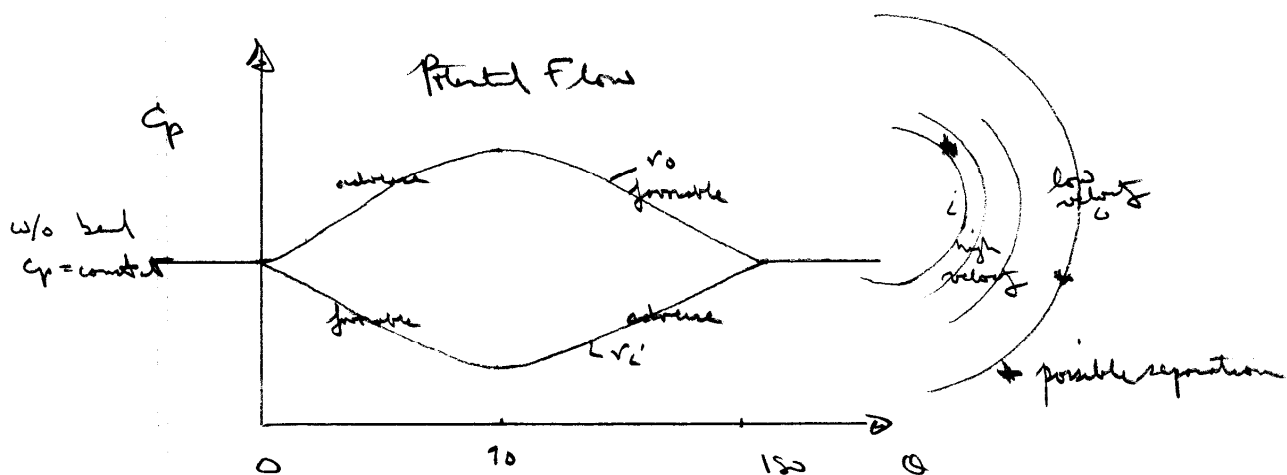


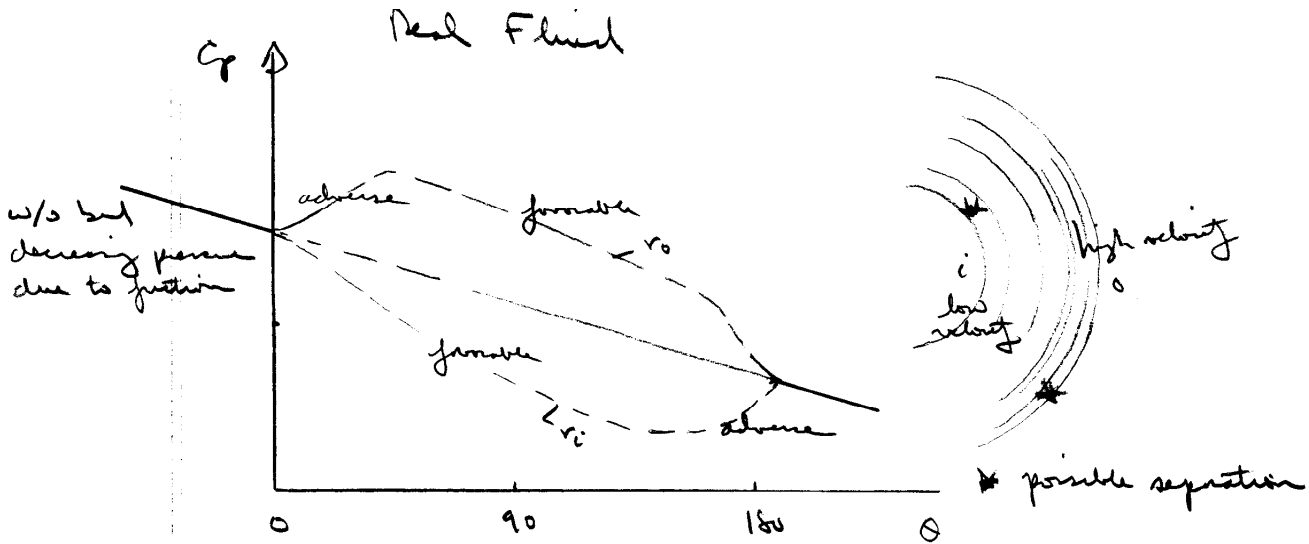
i.e.  $\frac{\partial p}{\partial r} > 0$  which is an adverse pressure gradient in  $r$  direction. The slower moving fluid near wall responds first and a swirling flow pattern results.



This swirling flow represents an energy loss which must be added to the  $h_L$ .

Also, flow separation can result due to adverse longitudinal pressure gradients which will result in additional losses.



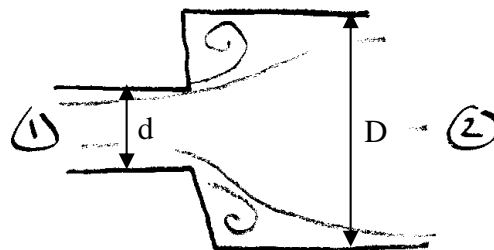


This shows potential flow is not a good approximate in internal flows (except possibly near entrance)

2. Valves: enormous losses
3. Entrances: depends on rounding of entrance
4. Exit (to a large reservoir):  $K = 1$   
i.e., all velocity head is lost
5. Contractions and Expansions  
sudden or gradual

theory for expansion:

$$h_L = \frac{(V_1 - V_2)^2}{2g}$$

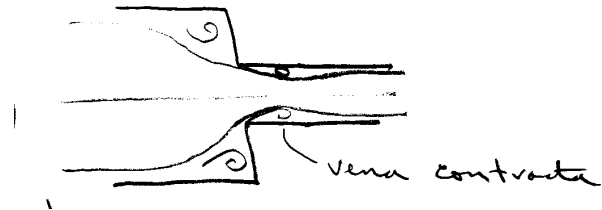


from continuity, momentum, and energy  
 (assuming  $p = p_1$  in separation pockets)

$$\Rightarrow K_{SE} = \left(1 - \frac{d^2}{D^2}\right)^2 = \frac{h_m}{V_1^2 / 2g}$$

no theory for contraction:

$$K_{SC} = .42 \left(1 - \frac{d^2}{D^2}\right)$$



from experiment

If the contraction or expansion is gradual the losses are quite different. A gradual expansion is called a diffuser. Diffusers are designed with the intent of raising the static pressure.

$$C_p = \frac{p_2 - p_1}{\frac{1}{2}\rho V_1^2}$$

$$C_{P_{ideal}} = 1 - \left(\frac{A_1}{A_2}\right)^2$$

Bernoulli and  
 continuity equation

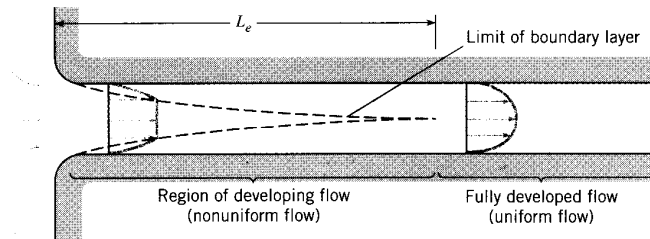
$$K = \frac{h_m}{V^2 / 2g} = C_{P_{ideal}} - C_p \quad \text{Energy equation}$$

Actually very complex flow and

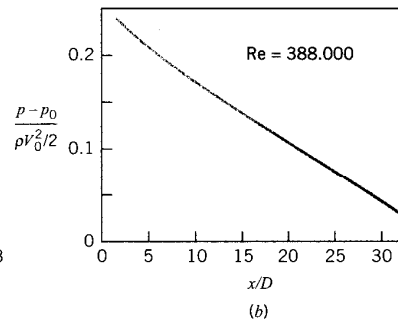
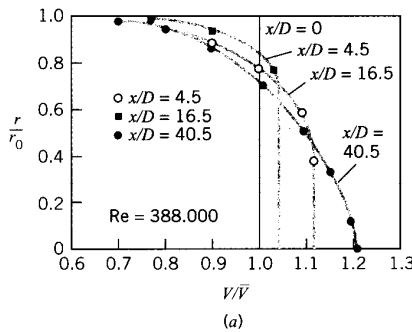
$$C_p = C_p \text{ (geometry, inlet flow conditions)}$$

i.e., fully developed (long pipe) reduces  $C_p$   
 thin boundary layer (short pipe) high  $C_p$   
 (more uniform inlet profile)

**FIGURE 10.10**  
 Flow characteristics at a pipe inlet (not to scale).

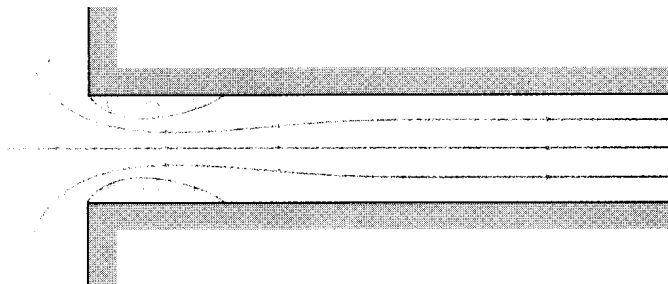


**FIGURE 10.11**  
 Distribution of velocity and pressure in the inlet region of a pipe [Barbin and Jones (3)].  
 (a) Velocity distribution.  
 (b) Pressure distribution.



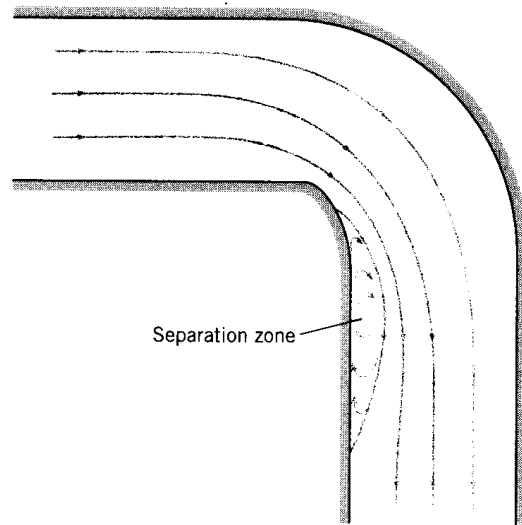
Turbulent flow

**FIGURE 10.12**  
 Flow at a sharp-edged inlet.



$K = .5$

FIGURE 10.13  
*Flow pattern in an  
elbow.*



See textbook Table 8.2 for a table of the loss coefficients  
for pipe components



TABLE 10.2 LOSS COEFFICIENTS FOR VARIOUS TRANSITIONS AND FITTINGS

| Description                         | Sketch                | Additional Data | $K$                          | Source                        |     |
|-------------------------------------|-----------------------|-----------------|------------------------------|-------------------------------|-----|
| Pipe entrance<br>$h_L = K_e V^2/2g$ |                       | $r/d$           | $K_e$                        | (2)*                          |     |
|                                     |                       | 0.0             | 0.50                         |                               |     |
|                                     |                       | 0.1             | 0.12                         |                               |     |
|                                     |                       | >0.2            | 0.03                         |                               |     |
| Contraction<br>$h_L = K_C V_2^2/2g$ |                       | $D_2/D_1$       | $K_C$<br>$\theta = 60^\circ$ | $K_C$<br>$\theta = 180^\circ$ | (2) |
|                                     |                       | 0.0             | 0.08                         | 0.50                          |     |
|                                     |                       | 0.20            | 0.08                         | 0.49                          |     |
|                                     |                       | 0.40            | 0.07                         | 0.42                          |     |
|                                     |                       | 0.60            | 0.06                         | 0.27                          |     |
|                                     |                       | 0.80            | 0.06                         | 0.20                          |     |
|                                     |                       | 0.90            | 0.06                         | 0.10                          |     |
| Expansion<br>$h_L = K_E V_1^2/2g$   |                       | $D_1/D_2$       | $K_E$<br>$\theta = 20^\circ$ | $K_E$<br>$\theta = 180^\circ$ | (2) |
|                                     |                       | 0.0             |                              | 1.00                          |     |
|                                     |                       | 0.20            | 0.30                         | 0.87                          |     |
|                                     |                       | 0.40            | 0.25                         | 0.70                          |     |
|                                     |                       | 0.60            | 0.15                         | 0.41                          |     |
|                                     |                       | 0.80            | 0.10                         | 0.15                          |     |
| 90° miter bend                      |                       | Without vanes   | $K_b = 1.1$                  | (37)                          |     |
|                                     |                       | With vanes      | $K_b = 0.2$                  | (37)                          |     |
| 90° smooth bend                     |                       | $r/d$           |                              | (5) and (19)                  |     |
|                                     |                       | 1               | $K_b = 0.35$                 |                               |     |
|                                     |                       | 2               | 0.19                         |                               |     |
|                                     |                       | 4               | 0.16                         |                               |     |
|                                     |                       | 6               | 0.21                         |                               |     |
|                                     |                       | 8               | 0.28                         |                               |     |
| 10                                  | 0.32                  |                 |                              |                               |     |
| Threaded pipe fittings              | Globe valve—wide open | $K_v = 10.0$    |                              | (37)                          |     |
|                                     | Angle valve—wide open | $K_v = 5.0$     |                              |                               |     |
|                                     | Gate valve—wide open  | $K_v = 0.2$     |                              |                               |     |
|                                     | Gate valve—half open  | $K_v = 5.6$     |                              |                               |     |
|                                     | Return bend           | $K_b = 2.2$     |                              |                               |     |
|                                     | Tee                   |                 |                              |                               |     |
|                                     | straight-through flow | $K_t = 0.4$     |                              |                               |     |
|                                     | side-outlet flow      | $K_t = 1.8$     |                              |                               |     |
| 90° elbow                           | $K_b = 0.9$           |                 |                              |                               |     |
| 45° elbow                           | $K_b = 0.4$           |                 |                              |                               |     |

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FIGURE 10.14  
*EGL and HGL at a sharp-edged pipe entrance.*

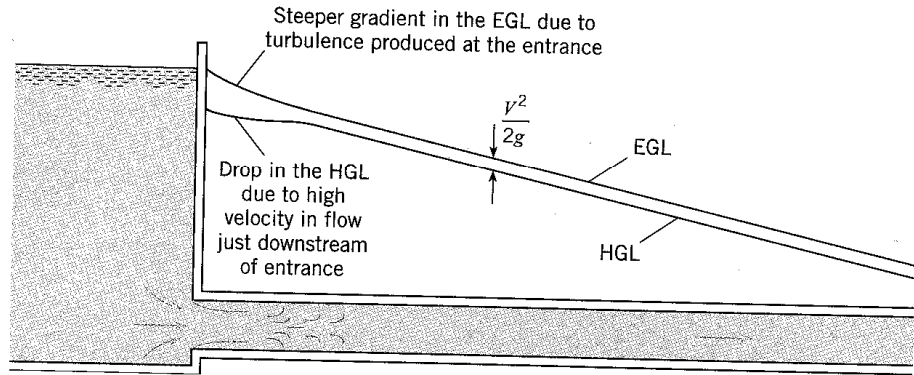


FIGURE 10.15  
*Head losses in a pipe.*

