

8.94

8.94 When the pump shown in Fig. P8.94 adds 0.2 horsepower to the flowing water, the pressures indicated by the two gages are equal. Determine the flowrate.

Length of pipe between gages = 60 ft

Pipe diameter = 0.1 ft

Pipe friction factor = 0.03

Filter loss coefficient = 12

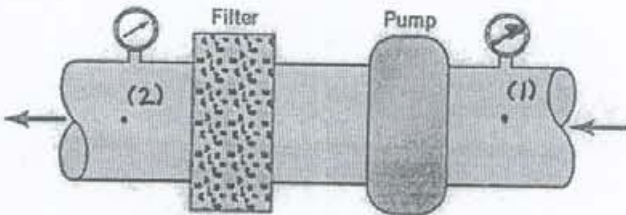


FIGURE P8.94

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 + h_p = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + h_L$$

$$P_1 = P_2, z_1 = z_2, V_1 = V_2$$

$$\text{So, } h_p = h_L \quad (1)$$

The pump adds 0.2 hp of power.

$$\dot{W} = 0.2 \text{ hp} \times \frac{550 \frac{\text{ft} \cdot \text{lb}}{\text{s}}}{1 \text{ hp}} = 110 \frac{\text{ft} \cdot \text{lb}}{\text{s}}$$

Convert to head by:

$$h_p = \frac{\dot{W}}{\gamma Q} = \frac{110 \frac{\text{ft} \cdot \text{lb}}{\text{s}}}{62.4 \frac{\text{lb}}{\text{ft}^3} Q} = \frac{1.76}{Q}$$

Sub into (1)

$$\frac{1.76}{Q} = \left(f \frac{L}{D} + \sum K_L \right) \frac{V^2}{2g} = \left(f \frac{L}{D} + \sum K_L \right) \frac{(Q/A)^2}{2g}$$

$$\text{or } Q^3 = \frac{1.76 (2)(g) A^2}{\left(f \frac{L}{D} + \sum K_L \right)} \quad \text{where } A = \frac{\pi}{4} (0.1 \text{ ft})^2 = 7.85 \times 10^{-3} \text{ ft}^2$$

$$= \frac{1.76 (64.4) (7.85 \times 10^{-3})^2}{\left(0.03 \frac{60}{0.1} + 12 \right)}$$

$$Q^3 = 2.328 \times 10^{-4}$$

$$\underline{\underline{Q = 0.0615 \text{ ft}^3/\text{s}}}$$