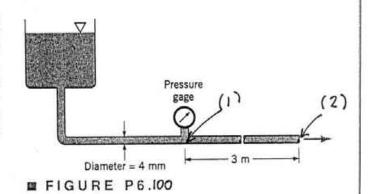
6.100 A simple flow system to be used for steady flow tests consists of a constant head tank connected to a length of 4-mm-diameter tubing as shown in Fig. P6.100. The liquid has a viscosity of $0.015 \text{ N} \cdot \text{s/m}^2$, a density of 1200 kg/m^3 , and discharges into the atmosphere with a mean velocity of 2 m/s. (a) Verify that the flow will be laminar. (b) The flow is fully developed in the last 3 m of the tube. What is the pressure at the pressure gage? (c) What is the magnitude of the wall shearing stress, τ_{rs} , in the fully developed region?



(a) Check Reynolds number to determine if flow is laminar:
$$Re = \frac{PV(2R)}{\mu} = \frac{(1200 \frac{k_B^2}{m^3})(2\frac{m}{s})(0.004m)}{0.015 \frac{N.5}{m^2}} = 640$$

Since the Reynolds number is well below 2100 the flow is laminar.

(b) For laminar flow,

$$V = \frac{R^2}{8\mu} \frac{\Delta p}{2}$$
(Eg. 6.152)

Since
$$\Delta p = P_1 - P_2 = P_1 - 0$$
 (see figure)
$$P_1 = \frac{8 \mu V l}{R^2} = \frac{8 (0.015 \frac{N.5}{m^2}) (2 \frac{m}{5}) (3 m)}{(0.004 m)^2} = \frac{180 k R}{100 k R}$$

(c)
$$T_{rz} = \mu \left(\frac{\partial V_r}{\partial z} + \frac{\partial V_z}{\partial r} \right)$$
 (Eq. 6.126f) For fully developed pipe flow, $V_r = 0$, so that

$$T_{rz} = \mu \frac{\partial v_{\overline{z}}}{\partial r}$$
Also,
$$V_{\overline{z}} = V_{max} \left[1 - \left(\frac{\Gamma}{R} \right)^2 \right]$$
(Eq. 6.154)

and with $v_{max} = 2V$, where V is the mean velocity $T_{rz} = 2V\mu\left(-\frac{2r}{R^2}\right)$

Thus, at the wall,
$$r = R$$
, $\left| \left(\frac{2 \frac{m}{5}}{R} \right) \left(0.015 \frac{N.5}{m^2} \right) \right| = \frac{60.0 \frac{N}{m^2}}{(0.004 m)}$