

December 10, 2014

NAME

Fluids-ID

Quiz 14. A smooth 0.10-m-diameter cork ball ($SG = 0.21$) is tied to an object on the bottom of a river as is shown in Figure 2. The flow speed U is 1.12 m/s. Neglect the string drag. Determine (a) buoyancy force B , (b) weight W , and (c) drag force on cork ball D_f (Hint: $D_f = \frac{1}{2} \rho U^2 A C_D$). (d) Calculate angle θ (Hint: Use $\sum F_x = 0$ and $\sum F_y = 0$).

$$(\rho_{\text{water}} = 998 \text{ kg/m}^3, \nu_{\text{water}} = 1.12 \times 10^{-6} \text{ m}^2/\text{s}, V_{\text{sphere}} = \frac{4}{3} \pi R^3)$$

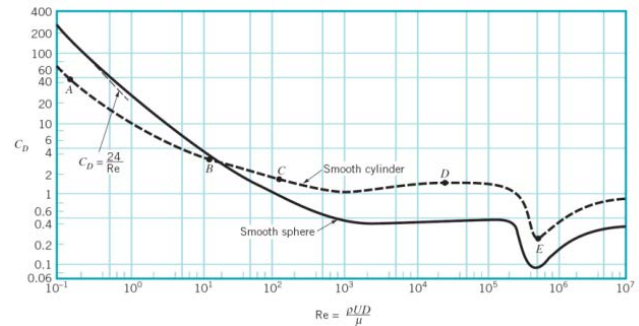


Figure 1 - Drag coefficient C_D as a function of Reynolds number Re

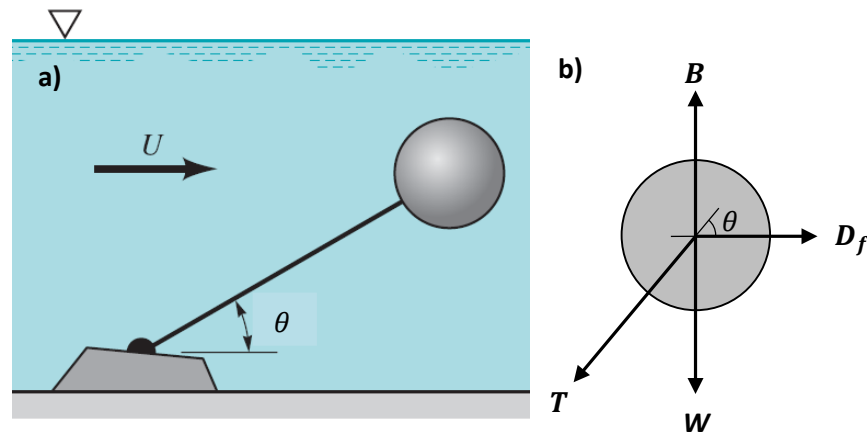


Figure 2 - (a) Schematic and (b) free body diagram for cork ball

Note: Attendance (+2 points), format (+1 point)

Solution:

a) Buoyancy force

$$B = \gamma V = \gamma \frac{4}{3} \pi R^3 = (998 \text{ kg/m}^3)(9.81 \text{ m/s}^2) \left(\frac{4\pi}{3} \right) \left(\frac{0.1 \text{ m}}{2} \right)^3 = 5.126 \text{ N}$$

(+1 point)

b) Weight

$$W = \gamma_{\text{cork}} V = \left(\frac{\gamma_{\text{cork}}}{\gamma} \right) \gamma V = SG \cdot B = 0.21 \times 5.126 \text{ N} = 1.077 \text{ N}$$

(+1 point)

c) Calculating drag force

$$Re = \frac{UD}{\nu} = \frac{(1.12 \text{ m/s})(0.1 \text{ m})}{1.12 \times 10^{-6} \text{ m}^2/\text{s}} = 1 \times 10^5$$

(+1 points)

From figure 7, $C_D = 0.5$ at $Re_D = 10^5$

(+1 points)

$$D_f = \frac{1}{2} \rho U^2 A C_D$$

$$D_f = \frac{1}{2} (998 \text{ kg/m}^3) (1.12 \text{ m/s})^2 \left(\frac{\pi}{4}\right) (0.1 \text{ m})^2 (0.5) = 2.458 \text{ N}$$

(+2 point)

d) Calculating angle θ

$$\sum F_x = 0 : T \cos \theta = D \quad (1)$$

$$\sum F_y = 0 : T \sin \theta = B - W \quad (2)$$

Dividing equation (2) by equation (1)

$$\tan \theta = \frac{B - W}{D}$$

$$\theta = \tan^{-1} \frac{B - W}{D} = \tan^{-1} \frac{5.126 \text{ N} - 1.077 \text{ N}}{2.458 \text{ N}} = \mathbf{58.7^\circ}$$

(+1 point)