

December 3, 2007

Quiz 8

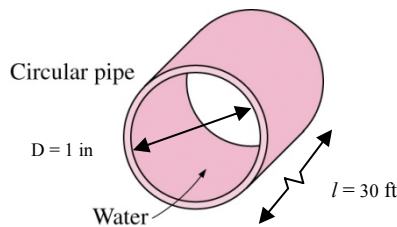
NAME _____

Student ID _____

Known: Water flows horizontally through a 1 inch inner diameter pipe over a length of 30 feet. Water has the following properties: $\nu = 1.21 \times 10^{-5} \text{ ft}^2/\text{s}$ and $\rho = 1.94 \text{ slug}/\text{ft}^3$. The equivalent roughness of the pipe, $\epsilon = 0.0001 \text{ ft}$.

Find: Part 1: Determine the friction factor and the pressure drop if the average velocity is 0.2 ft/second.
Part 2: Determine the friction factor and the pressure drop if the average velocity is 1 ft/second.

Assumptions: 1) The flow is fully developed. 2) No change in elevation. 3) There are no bends or contractions.



Solution:

Equations:

$$Re = VD/\nu$$

$$\frac{1}{\sqrt{f_{turb}}} = -2 \log \left(\frac{\epsilon/D}{3.7} + \frac{2.51}{Re \sqrt{f_{turb}}} \right)$$

$$f_{lam} = 64/Re$$

$$h_L = f \frac{LV^2}{2Dg}$$

$$\frac{p_1}{\gamma} + \alpha_1 \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\gamma} + \alpha_2 \frac{V_2^2}{2g} + z_2 + h_L$$

Part 1:

$$Re = VD/\nu = (0.2 \text{ ft/s}) (1/12 \text{ ft}) / (0.0000121 \text{ ft}^2/\text{s}) = 1,377$$

→ Laminar flow

$$f_{lam} = 64/Re = 64 / 1,377 = 0.0464$$

$$\frac{p_1}{\gamma} + \alpha_1 \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\gamma} + \alpha_2 \frac{V_2^2}{2g} + z_2 + h_L$$

$$\frac{p_1}{\gamma} = \frac{p_2}{\gamma} + h_L$$

$$\frac{p_1 - p_2}{\gamma} = h_L$$

$$p_1 - p_2 = \gamma h_L$$

December 3, 2007

Quiz 8

$$\Delta p = \gamma h_L = \rho g f \frac{LV^2}{2Dg} = f \frac{\rho LV^2}{2D} = 0.0464 \times \frac{1.94 \frac{\text{slug}}{\text{ft}^3} \times 30 \text{ ft} \times 0.2 \frac{\text{ft}}{\text{s}}}{2 \times (1/12) \text{ ft}} = 0.649 \frac{\text{lb}}{\text{ft}^2} = 0.0045 \frac{\text{lb}}{\text{in}^2}$$

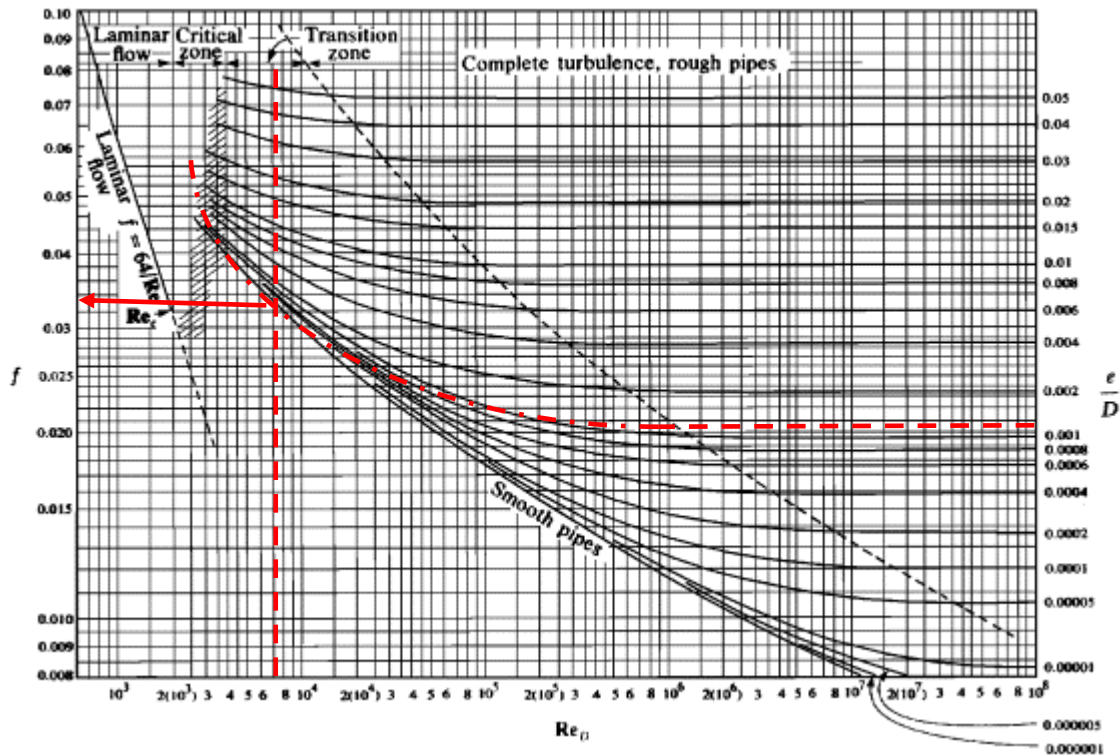
Part 2:

$$Re = VD/v = (1 \text{ ft/s}) (1/12 \text{ ft}) / (0.0000121 \text{ ft}^2/\text{s}) = 6887$$

➔ Turbulent flow

➔ Go to Moody diagram or Colebrook friction factor equation

$$\varepsilon/D = 0.0001 \text{ ft} / (1/12 \text{ ft}) = 0.0012$$



$$f_{\text{urb}} \sim 0.035$$

$$\Delta p = \gamma h_L = \rho g f \frac{LV^2}{2Dg} = f \frac{\rho LV^2}{2D} = 0.035 \times \frac{1.94 \frac{\text{slug}}{\text{ft}^3} \times 30 \text{ ft} \times 1 \frac{\text{ft}}{\text{s}}}{2 \times (1/12) \text{ ft}} = 12.2 \frac{\text{lb}}{\text{ft}^2} = 0.0850 \frac{\text{lb}}{\text{in}^2}$$