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Suppose that glycerin is flowing ($T = 20^{\circ}$ C) and that the pressure gradient dp/dx is $-1.6kN/m^3$. What are the shear stress and velocity at the lower wall (y = 0) if the space *B* between the walls is 5.0*cm*? The velocity distribution for viscous flow between stationary plates is

$$u = -\frac{1}{2\mu} \frac{dp}{dx} \left(By - y^2 \right)$$



Solution:

At the lower wall, y = 0

$$u_{y=0} = -\frac{1}{2\mu} \frac{dp}{dx} (By - y^2) = 0$$

$$\frac{du}{dy} = -\frac{1}{2\mu} \frac{dp}{dx} (B - 2y)$$

$$\tau = \mu \frac{du}{dy} = -\frac{1}{2} \frac{dp}{dx} (B - 2y)$$

$$\tau_{y=0} = -\frac{1}{2} \times (-1.6) \times (0.05 - 0) = 0.04 N/m^2$$