

3.113

3.113 Water flows in a rectangular channel that is 2.0 m wide as shown in Fig. P3.113. The upstream depth is 70 mm. The water surface rises 40 mm as it passes over a portion where the channel bottom rises 10 mm. If viscous effects are negligible, what is the flowrate?

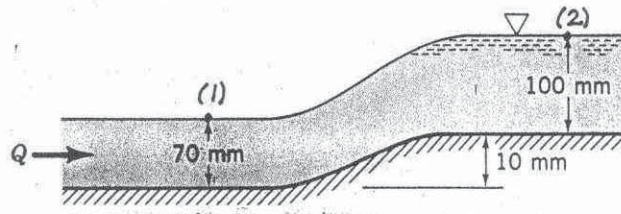


FIGURE P3.113

$$\frac{p_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{p_2}{\gamma} + \frac{V_2^2}{2g} + z_2 \quad \text{where } p_1 = 0, p_2 = 0, z_1 = 0.07 \text{ m, (1)}$$

$$\text{and } z_2 = (0.01 + 0.10) \text{ m} = 0.11 \text{ m}$$

$$\text{Also, } A_1 V_1 = A_2 V_2$$

or

$$V_2 = \frac{h_1}{h_2} V_1 = \frac{0.07 \text{ m}}{0.10 \text{ m}} V_1 = 0.7 V_1$$

Thus, Eq. (1) becomes

$$[1 - 0.7^2] V_1^2 = 2(9.81 \frac{\text{m}}{\text{s}^2})(0.11 - 0.07) \text{ m} \quad \text{or } V_1 = 1.24 \frac{\text{m}}{\text{s}}$$

Hence,

$$Q = A_1 V_1 = (0.07 \text{ m})(2.0 \text{ m})(1.24 \frac{\text{m}}{\text{s}}) = \underline{\underline{0.174 \frac{\text{m}^3}{\text{s}}}}$$