1. Purpose

The purpose of this investigation is to provide Hands-on experience using a table-top facility and simple measurement systems to obtain fluid property measurements (density and kinematic viscosity), comparing results with manufacturer values, and implementing standard EFD uncertainty analysis. Additionally, this laboratory will provide an introduction to camera settings and flow visualization for the ePIV system with a circular cylinder model.

2. Experimental Design

2.1 Part 1: For Determination of Fluid Properties

Common methods used for determining viscosity include the rotating-concentric-cylinder method (Engler viscosimeter) and the capillary-flow method (Saybolt viscosimeter). In the present experiment we will measure the kinematic viscosity through its effect on a falling object in still fluid (figure 1). The maximum velocity attained by an object in free fall (terminal velocity) is inversely proportional to the viscosity of the fluid through which it is falling. When terminal velocity is attained, the body experiences no acceleration, and so the forces acting on the body are in equilibrium.

![Figure 1. Schematic of the experimental setup](image)

The forces acting on the body are the gravitational force,

\[ F_g = mg = \rho_{sphere} \pi \frac{D^3}{6} g \]  

(1)

the force due to buoyancy,

\[ F_b = \rho_{fluid} \pi \frac{D^3}{6} g \]  

(2)

and the drag force, the resistance of the fluid to the motion of the body, which is similar to friction. For \( Re \ll 1 \) (\( Re \) is the Reynolds number, defined as \( Re = \frac{VD}{\nu} \)), the drag force on a sphere is described by the Stokes expression,

\[ F_d = 3 \rho_{fluid} \pi \nu V D \]  

(3)

where, \( D \) is the sphere diameter, \( \rho_{fluid} \) is the density of the fluid, \( \rho_{sphere} \) is the density of the falling sphere, \( \nu \) is the kinematic viscosity of the fluid, \( V \) is the velocity of the sphere through the fluid (in this case, the terminal velocity), and \( g \) is the acceleration due to gravity (White 1994).

Once terminal velocity is achieved, a summation of the vertical forces must balance. This gives:

\[ \nu = \left( \frac{D^2 g (\rho_{sphere} / \rho_{fluid} - 1)t}{18 \lambda} \right) \]  

(4)

where \( t \) is the time taken for the sphere to fall the vertical distance \( \lambda \).

Using equation (4) for two different materials, Teflon and steel spheres, the following relationship for the
density of the fluid is obtained, where subscripts \( s \) and \( t \) refer to the steel and Teflon spheres, respectively.

\[
\rho_{\text{fluid}} = \frac{(D_s^2 \ t_s \ - \ D_t^2 \ t_t \ \rho_s)}{(D_s^2 \ t_s \ - \ D_t^2 \ t_t)} \quad (5)
\]

In this experiment, we will drop spheres (Steel and Teflon), each set of spheres having a different density and diameter, through a long transparent cylinder filled with glycerin (Figure 1). Two horizontal lines are marked on the vertical cylinder. The sphere will reach terminal velocity before entering this region, and will fall between these two lines at constant velocity. We will measure the time required for the sphere to fall through the distance \( \lambda \). The measurement system includes:

- A transparent cylinder (beaker) containing glycerin
- A scale to measure the distance the sphere has fallen
- Steel and Teflon spheres of different diameters
- A stopwatch to measure fall time
- A micrometer to measure sphere diameter
- A thermometer to measure room temperature

An Excel worksheet (Lab1_Data_Reduction_Sheet under “EFD Lab1”) is provided on class website (http://css.engineering.uiowa.edu/~fluids) to facilitate data acquisition, data reduction, and uncertainty analysis.

2.2 Part 2: For Flow Visualization using ePIV

Particle image velocimetry, or PIV, is an advanced experimental method used for measuring the velocity field in fluid flow. In PIV, a fluid is seeded with small particles which have similar density to the fluid, so that the particles are able to follow the fluid motion. A laser sheet is shone through the flow being observed, causing the seeding particles to be illuminated, and a camera is used to take rapid photographs of the seeded fluid. Software is used to analyze the images captured, tracking the motion of the seeding particles to determine the fluid velocity at all points in the illuminated plane.

This laboratory involves an Educational PIV system, or ePIV system, which is capable of performing PIV analysis on a small scale, using water. The ePIV system consists of:

- A box, to house all of the physical components
- A closed-circuit flow channel, in which different model geometries can be inserted for testing
- A variable-speed pump, to drive the water through the system
- A reservoir that holds the seeded fluid that is pumped through the system
- A Class II laser, used to illuminate the seeded flow
- A camera, which transmits captured images to a computer
- A computer, with software to capture images and perform PIV analysis

In addition to performing PIV calculations, the ePIV system can be used for flow visualization, and it is for this purpose that the system will be used in this investigation. The ePIV system will be fitted with a circular cylinder insert and streamlines will be observed for different Reynolds numbers, \( Re = \frac{VD}{\nu} \), where \( V \) is the fluid velocity, \( D \) is the cylinder diameter, and \( \nu \) is the kinematic viscosity of water. For the circular cylinder, the ePIV device can generate Reynolds numbers ranging from approximately 2 to 90.

A number of camera parameters can be modified, using the provided “Camera Control” software, to achieve optimal flow visualization settings. In this laboratory, the following parameters will be adjusted:

- Brightness – This controls the overall brightness of the image. For the best flow visualization results, brightness should be set to a medium-high value
- Contrast – This controls the contrast ratio of the image. This should be adjusted to provide clear distinction between seeding particles and the background of the image
- Exposure – This controls how long the camera sensors are exposed per image frame taken. Higher values correspond to shorter exposure times, and lower values correspond to longer exposure times. The longer the sensors are exposed per frame, the brighter the image, and the more the individual particles will visually appear to stretch, showing an approximation of flow streamlines.
- Gain – This controls the sensitivity of the sensors per unit time. Using higher gain will amplify the signal obtained by the sensors, so typically higher gain values are needed for images taken with short exposure times, which would otherwise be very dark.
- Focus – This controls the camera focus. It should be set to provide the sharpest possible image.

3. Experimental Process
3.1 Part 1: Determination of Fluid Properties
The diagram of the experimental process is provided in Figure 2.

3.1.1 Test Setup
Before starting the experiment, verify that the cylinder is vertical and then open the cylinder lid. Prepare 10 Teflon and 10 Steel spheres, making sure that the spheres are clean. Test the functionality of the stopwatch, micrometer, and thermometer.

3.1.2 Data Acquisition
The experiment procedure follows the sequence described below:
1. Measure the temperature of the room.
2. Measure the distance between the two lines, \( \lambda \).
3. Measure the diameter of the first sphere (teflon or steel) using the micrometer.
4. Release the sphere at the surface of the fluid in the cylinder.
5. Once the sphere has settled, release the gate handle to begin the sphere’s descent.
6. Measure the time taken for each sphere to travel the distance \( \lambda \).
7. Repeat steps 3-6 for 10 spheres of each material.

Since the fall time of the sphere is very short, it is important to measure the time as accurately as possible. Start the stopwatch as soon as the bottom of the ball hits the first mark on the cylinder, and stop it as soon as the
bottom of the ball hits the second mark. Two people should cooperate in this measurement with one observing the first mark and handling the stopwatch, and the other observing the second mark. A spreadsheet should be created for data acquisition, following the example shown in Figure 3, below. The data from your spreadsheet will later be inserted into Lab1_Data_Reduction_Sheet for data reduction and uncertainty analysis.

<table>
<thead>
<tr>
<th>Trial</th>
<th>Teflon</th>
<th>Steel</th>
<th>Results</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$B_i$</td>
<td>$t_i$</td>
<td>$D_i$</td>
</tr>
<tr>
<td>1</td>
<td>(m)</td>
<td>(sec)</td>
<td>(m)</td>
</tr>
<tr>
<td>2</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td></td>
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<td></td>
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<tr>
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<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Average</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 3. Sample data acquisition spreadsheet

3.1.3 Data Reduction

Figure 2 illustrates the block diagram of the measurement systems and data reduction equations for the results. Use Lab1_Data_Reduction_Sheet for the data reduction procedure after importing the data from your spreadsheet.

Data reduction includes the following steps:
1. Calculate the statistics (mean and standard deviations) of the repeated measurements.
2. Calculate the fluid density for each individual measurement using equation (5).
3. Calculate the kinematic viscosity for each individual measurement using equation (4).

3.1.4 Uncertainty Analysis

Uncertainties for the experimentally-determined glycerin density and kinematic viscosity will be evaluated using Lab1_Data_Reduction_Sheet. The methodology for estimating uncertainties follows the AIAA S-071-1995 Standard (AIAA, 1995) as summarized in Stern et al. (1999), for multiple tests. Figure 4 is a block diagram depicting error propagation methodology for the measured density and viscosity. The data reduction equations for density and viscosity of glycerin are equations (5) and (4), respectively. Using these data reduction equations, first, the elemental errors for each independent variable, $X_i$, should be identified using the best available information for bias errors, and using repeated measurements for precision errors. Table 1 contains a summary of the elemental bias errors assumed for the present experiment. For this investigation, we will neglect the contribution of correlated bias errors.

![Figure 4. Block diagram of the experiment, including measurement systems, data reduction equations, and results](image)

Table 1. Assessment of the bias limits for the independent variables

<table>
<thead>
<tr>
<th>Bias limit</th>
<th>Bias Limit</th>
<th>Estimation</th>
</tr>
</thead>
<tbody>
<tr>
<td>$B_{BD}$ = $B_{DS} = B_{DL}$</td>
<td>0.000005 m</td>
<td>$\frac{1}{2}$ instrument resolution</td>
</tr>
<tr>
<td>$B_{t}$ = $B_{Ds} = B_{Ht}$</td>
<td>0.01 s</td>
<td>Last significant digit</td>
</tr>
<tr>
<td>$B_\lambda$</td>
<td>0.00079 m</td>
<td>$\frac{1}{2}$ instrument resolution</td>
</tr>
</tbody>
</table>
### 3.1.4.1 UA for Density of Glycerin

The total uncertainty for the glycerin density measurement is:

\[
U_{\rho_G} = \sqrt{B_{\rho_G}^2 + P_{\rho_G}^2}
\]  

(6)

The bias limit \( B_{\rho_G} \), and the precision limit \( P_{\rho_G} \), for the result are given by:

\[
B_{\rho_G} = \sum_{i=1}^{j} \theta_i^B B_i^2 = \theta_i^B \rho_{iG} + \theta_i^B \rho_{iG} + \theta_i^B \rho_{iG} + 2\theta_i \theta_i \rho_{iG} B_{iG} + 2\theta_i \theta_i \rho_{iG} B_{iG}
\]  

(7)

\[
P_{\rho_G} = 2 \cdot S_{\rho_G} \sqrt{M}
\]  

(8)

where the sensitivity coefficients \( \theta \) (calculated using mean values for the independent variables) are:

\[
\theta_i = \frac{\partial \rho_i}{\partial D_i} = \frac{2D_i^2 t_i t_s D_i (\rho_{iG} - \rho_{iG})}{[D_i^2 t_i - D_i^2 t_s]^2} \left[ \frac{kg}{m^3} \right]
\]  

(9)

\[
\theta_i = \frac{\partial \rho_G}{\partial t_i} = \frac{D_i^2 t_i t_s (\rho_{iG} - \rho_{iG})}{[D_i^2 t_i - D_i^2 t_s]^2} \left[ \frac{kg}{m^3 \cdot s} \right]
\]  

(10)

Note that the bias limits for \( D_i \) and \( D_i \), as well as \( t_i \) and \( t_i \) are correlated because diameters and fall times for each set of spheres were measured with the same instrumentation. The last two terms of equation (7) represent these correlated bias errors. As previously mentioned, these terms will be neglected for this study. The standard deviation for density of glycerin is calculated using the following formula (where \( M = 10 \)):

\[
S_{\rho_G} = \left[ \sum_{k=1}^{m} (\rho_k - \bar{\rho})^2 \right]^{1/2}{M-1}
\]  

(13)

### 3.1.4.2 UA for Viscosity of Glycerin

Uncertainty assessment for the glycerin viscosity will be based on the measurements conducted with the teflon spheres, because the flow around the Teflon spheres is in better agreement with Stokes’ theorem \((Re \ll 1)\). The total uncertainty for the viscosity measurement is given by equation (24) in Stern et al. (1999), and is:

\[
U_v = \sqrt{B_v^2 + P_v^2}
\]  

(14)

The bias limit \( B_v \), and the precision limit \( P_v \), for viscosity (neglecting correlated bias errors) is given by equations (14) and (23) in Stern et al. (1999), respectively:

\[
B_v = \sum_{i=1}^{j} \theta_i^B B_i^2 = \theta_i^B \rho_{iG} + \theta_i^B \rho_{iG} + \theta_i^B \rho_{iG} + 2\theta_i \theta_i \rho_{iG} B_{iG} + 2\theta_i \theta_i \rho_{iG} B_{iG}
\]  

(15)

\[
P_v = 2 \cdot S_v \sqrt{M}
\]  

(16)

The bias limits for \( B_{\rho_i} \), \( \rho_{iG} \), and \( B_{\rho_i} \) were evaluated previously in conjunction with the estimation of \( U_{\rho_G} \). The value for \( B_v \) is provided in Table 1. The sensitivity coefficients, \( \theta \), are calculated with mean values, using the following equations:

\[
\theta_i = \frac{\partial \nu_i}{\partial D_i} = \frac{2D_i g (\rho_{iG} - 1)}{18 \lambda} \left[ \frac{m}{s} \right]
\]  

(17)

\[
\theta_i = \frac{\partial \nu_i}{\partial t_i} = \frac{D_i^2 g \rho_{iG} t_i}{18 \lambda \rho_{iG}^2} \left[ \frac{m^2}{s^2} \right]
\]  

(18)

\[
\theta_i = \frac{\partial \nu_i}{\partial \rho_{iG}} = \frac{D_i^2 g \rho_{iG} t_i}{18 \lambda \rho_{iG}^2} \left[ \frac{m^3}{kg \cdot s} \right]
\]  

(19)

\[
\theta_i = \frac{\partial \nu_i}{\partial \lambda} = \frac{D_i^2 g \rho_{iG} t_i}{18 \lambda^2} \left[ \frac{m}{s} \right]
\]  

(20)
Note that, unlike for density, there are no correlated bias errors contributing to the viscosity result, because only one set of sphere measurements were used. The standard deviation for the viscosity of glycerin, for $M=10$ repeated measurements, is calculated using the following formula:

$$S_{\nu} = \left( \frac{\sum_{k=1}^{M} (\nu_k - \nu)^2}{M - 1} \right)^{1/2}$$  \hspace{1cm} (21)$$

### 3.1.5 Data Analysis

The measured values from the completed `Lab1_Data_Reduction_Sheet` will be compared with benchmark data (Figure 5) based on information provided by the manufacturer. The following questions relate to fluid physics, the EFD process, and uncertainty analysis. **Answers should be included in the Lab report following the EFD lab report instructions and using the EFD lab report template (EFDlab1-Template.doc).**

1. What aspects of the present “hands-on” experiment would improve the accuracy of the results if the measurement system was automated?
2. Calculate the effective Reynolds numbers for our experiment, using $Re = VD/\nu << 1$, where $V$ is the sphere fall velocity, $D$ is the sphere diameter, and $\nu$ is the kinematic viscosity of the glycerin. Can we use Stokes’ equation for calculating the drag force acting on the spheres?
3. How does the viscosity of glycerin change with temperature, and why?
4. What is the major difference between estimating the bias and precision limits, given in equations (7) and (8), respectively?
5. If correlated bias errors are included, as given in equation (14), Stern et al. (1999), will this inclusion always increase the magnitude of the bias limit?

![Figure 5](image)

**Figure 5.** Reference data for the density and viscosity of 100% aqueous glycerin solutions (Proctor & Gamble Co., Product Catalogue, 1995)

### 3.2 Part 2: Flow Visualization using ePIV

#### 3.2.1 Test Setup

Prior to the experiment, your TA will set up the ePIV system with a circular cylinder model insert.

#### 3.2.2 Data Acquisition

The ePIV experimental procedure follows the steps listed below:

1. Turn on the ePIV system by flipping the power switch on the back of the device.
2. On the computer desktop, open the “Camera Control” software to display a live video feed from the ePIV device.
3. The software provides a variety of adjustable parameters. Using the software, adjust the brightness, contrast, exposure, gain, and focus settings until your image appears similar to the samples provided in Figure 6, below. You should be able to visualize streamlines. Record the values used for each camera parameter.
4. Once you have obtained the desired camera parameters, adjust the knob on the front of the ePIV system to modify flow speed. Observe how the flow changes over a range of velocities. Note especially the
wake region behind the cylinder. You will notice that the streamlines become less defined as the fluid velocity decreases.

5. Adjust the flow speed knob to obtain a visualization of high-velocity (high Reynolds number) flow. If necessary, re-adjust your camera parameters to obtain a clear image, and record the new values. Press the “capture image” button in the camera control window to save your image. This file will be saved to/home/usr. Find the file on the computer and copy it to a usb drive, saving it with a unique name. This file will be posted to the website and you will be notified.

6. Adjust the flow speed knob to obtain a visualization of low-velocity (low Reynolds number) flow. Readjust and record camera parameters, if necessary. Capture this image and give it a unique name as well, as you did in step 5.

3.2.3 Data Analysis

Your lab report should include the two images that you captured using the Camera Control software. Specify the camera settings used to capture each image. You should answer the following questions and include them as well:

1. What differences do you notice between the high and low Reynolds number flow images?
2. Using the sample images in Figure 6 as guidelines, what would you estimate the Reynolds number to be for each of your images?
3. The flow around the falling spheres tested in the first part of this laboratory follows Stokes’ theorem. Based on your ePIV flow observations for mass flow speeds, qualitatively plot streamlines around the circular cylinder for a low and high Reynolds numbers.
4. References

Visualization clips: [http://css.engineering.uiowa.edu/fluidslab/referenc/concepts.html](http://css.engineering.uiowa.edu/fluidslab/referenc/concepts.html) - Viscosity