57:022 Principles of Design II - Quiz \#7 Solutions
Spring 2002

Five components $(A, B, C, D, \& E)$ are available for constructing a system. The probability that each component survives the first year of operation is

- $70 \%$ for $\mathrm{A}, \mathrm{B}, \& \mathrm{C}$
- $80 \%$ for D \& E.

For each system (1) through (5) below:
For each of these three scenarios (a,b,c), indicate whether the system will Fail or Survive (write " $F$ " or " $S$ " in the table)::
(i) only components A and C fail.
(ii) only components B and D fail.
(iii) only components C, D, \& E fail.

| $\begin{gathered} \text { System } \\ \# \\ \hline \end{gathered}$ | Diagram | Scenario (i) | Scenario (ii) | Scenario (iii) | Reliability |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $-A-B-D-D-D-$ | F | F | F | d |
| 2 | $\left.\begin{array}{l} \sqrt{\mathrm{A}} \\ -\mathrm{B} \end{array}\right], \mathrm{D}_{-}$ | S | S | F | c |
| 3 | $-\mathrm{A}-\mathbf{C}$ | S | F | F | b |
| 4 | $-\sqrt{\mathrm{A}}, \stackrel{\mathrm{~B}}{\mathrm{D}}+\sqrt{\mathrm{E}}$ | S | F | F | h |
| 5 | $\left.-\mathrm{A}-\mathrm{B}-\boxed{\mathrm{C}}-\frac{\mathrm{D}}{[\mathrm{E}}\right]$ | F | F | F | e |

For each system (\#1-5) above, write the letter below indicating the computation of the 1-year reliability(i.e., survival probability):
a. $1-(0.3)^{3}(0.2)^{2}=0.99892$
f. $1-(0.3)^{3}\left[1-(0.8)^{2}\right]=0.99028$
b. $1-\left[1-(0.7)^{3}\right]\left[1-(0.8)^{2}\right]=0.76348$
g. $\left[1-(0.3)^{3}\right](0.2)^{2}=0.03892$
c. $\left[1-(0.3)^{3}\right]\left[1-(0.2)^{2}\right]=0.93408$
h. $\left[1-(0.3)^{3}\right](0.8)^{2}=0.62272$
d. $(0.7)^{3}(0.8)^{2}=0.21952$
i. $1-(0.3)^{3}\left[1-(0.8)^{2}\right]=0.99028$
e. $(0.7)^{3}\left[1-(0.2)^{2}\right]=0.32928$
j. None of the above

