************* 57:022 Principles of Design II - Quiz #7 Solutions Spring 2002 *****

Five components (A,B,C,D, & E) are available for constructing a system. The probability that each component *survives* the first year of operation is

- 70% for A, B, & C
- 80% for D & E.

For each system (1) through (5) below:

For each of these three scenarios (a,b,c), indicate whether the system will Fail or Survive (write "F" or "S" in the table)::

- (i) only components A and C fail.
- (ii) only components B and D fail.
- (iii) only components C, D, & E fail.

System	Diagram	Scenario	Scenario	Scenario	
#		(i)	(ii)	(iii)	Reliability
1	——A—B—C—D—E—	F	F	F	d
2	A D E	S	S	F	c
3	A B C D E	S	F	F	b
4	B D E	S	F	F	h
5	-A-B-C-E	F	F	F	e

For each system (#1-5) above, write the letter below indicating the *computation* of the 1-year reliability (i.e., survival probability):

a.
$$1 - (0.3)^3(0.2)^2 = 0.99892$$

b.
$$1 - [1 - (0.7)^3][1 - (0.8)^2] = 0.76348$$

b.
$$1 - [1 - (0.7)^3][1 - (0.8)^2] = 0.76348$$

c. $[1 - (0.3)^3][1 - (0.2)^2] = 0.93408$
d. $(0.7)^3(0.8)^2 = 0.21952$

d.
$$(0.7)^3(0.8)^2 = 0.21952$$

e.
$$(0.7)^3[1-(0.2)^2] = 0.32928$$

f.
$$1 - (0.3)^3[1 - (0.8)^2] = 0.99028$$

g.
$$[1 - (0.3)^3](0.2)^2 = 0.03892$$

h.
$$[1 - (0.3)^3] (0.8)^2 = 0.62272$$

i.
$$1 - (0.3)^3[1 - (0.8)^2] = 0.99028$$

j. None of the above