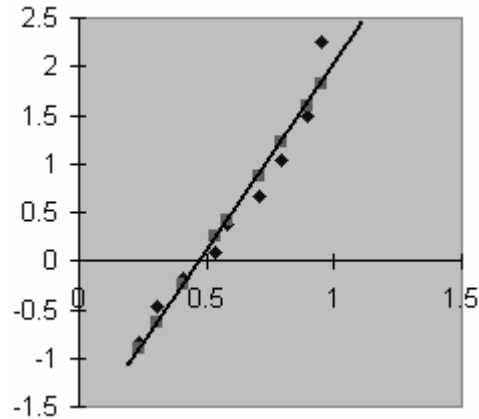


10. If the arrival process *does* have the assumed distribution, then $P\{D \geq \underline{\quad ? \quad}\} = 10\%$ (choose nearest value)
 a. ≤ 7 b. 8 c. 9 d. 10 e. 11 f. 12 g. 13 h. ≥ 14

Part IV. An electronic device is made up of a large number of redundant components, and the device fails when the last component fails. The lifetime of each component is random, but its probability distribution is unknown. The manufacturer has provided a 90-day (or 3-month) warranty on this device.

A test of the device is performed, in which *ten* units of the device are operated simultaneously, and the time of the first *nine* failures is recorded. The failure time **T** (in years), and the fraction **F** of the devices which have failed at time **T** are shown in the table, together with $-\ln(-\ln F)$:

T	F	$-\ln(-\ln F)$
0.233	0.1	-0.8340
0.304	0.2	-0.4759
0.408	0.3	-0.1856
0.537	0.4	0.0874
0.579	0.5	0.3665
0.703	0.6	0.6717
0.792	0.7	1.0309
0.895	0.8	1.4999
0.953	0.9	2.2504



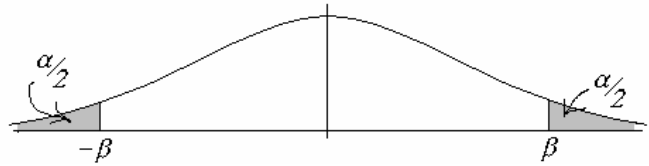
We will make the assumption that the unit's lifetime has a *Gumbel* distribution. In order to estimate the parameters α and u , a linear regression was performed, using the data in the table above, with the resulting equation:

$$(-\ln(-\ln F)) = 3.77T - 1.77$$

1. Based upon the above linear fit, the value of the "shape" parameter (α) of the probability distribution is approximately (choose nearest value).
 a. 0 b. 0.5 c. 1.0 d. 2.0 e. 3.0 f. 4.0 g. 5.0
2. Based upon the above linear fit, the value of the "location" parameter (u) of the probability distribution is approximately (choose nearest value).
 a. 0 b. 0.5 c. 1.0 d. 2.0 e. 3.0 f. 4.0 g. 5.0
3. The percent of the units which are expected to fail during the 90-day warranty period is (choose nearest value):
 a. 1% b. 2% c. 3% d. 4% e. 5% f. 6%
 g. 7% h. 8% i. 9% j. 10% k. 11% l. $\geq 12\%$
4. The expected lifetime of the unit (in years) is (choose nearest value):
 a. 0.1 b. 0.2 c. 0.3 d. 0.4 e. 0.5 f. 0.6
 g. 0.7 h. 0.8 i. 0.9 j. 1.0 k. 1.1 l. ≥ 1.2
5. To simulate values of **T** having this distribution, one might use...
 a. Inverse transformation method b. Rejection method
 c. Both a & b are correct d. Neither a nor b are correct.

Student's t-distribution: β such that total shaded area = α

Degrees of freedom	$\alpha=10\%$	$\alpha=5\%$	$\alpha=1\%$
1	6.314	12.706	63.657
2	2.920	4.303	9.925
3	2.353	3.182	5.841
4	2.132	2.776	4.604
5	2.015	2.571	4.032
6	1.943	2.447	3.707
7	1.895	2.365	3.499



Chi-square distribution: χ^2 such that $P\{D \geq \chi^2\} = \alpha$

Degrees of freedom	$\alpha=10\%$	$\alpha=5\%$	$\alpha=1\%$
1	2.706	3.841	6.635
2	4.605	5.991	9.210
3	6.251	7.815	11.345
4	7.779	9.488	13.277
5	9.236	11.070	15.086
6	10.645	12.592	16.812
7	12.017	14.067	18.475

