Tandem Stations with Blocking	<ul> <li>A job which completes processing at the first station when the second station is busy will remain at the first station, "blocking it", i.e., preventing it from accepting a new job.</li> <li>Compute the steady-state probabilities.</li> <li>Compute the throughput rate for the system.</li> </ul>		
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A processing system is composed of <b>two stations in tandem</b> . • The arrival of jobs at station #1 is a Poisson process with a rate of 4/hour, but station #1 can accept jobs only when it is idle. • The processing time at each station is exponentially distributed with a mean of 10 minutes. • There is room in the system for only two jobs, one at each station. • No queueing between stations or before the first station is permitted.	The state of the system is 2- dimensional: denote the state of each station by 0) idle 1) busy and, for station #1, b) "blocked". The possible states of the system are therefore 1. $(0,0)$ 2. $(1,0)$ 3. $(0,1)$ 4. $(1,1)$ 5. $(b,1)$		
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Trai	nsiti	on	Rate	a Ma	trix		Steady-state equations:
00 10 01 11 b1	00 -4 0 0 0	<b>10</b> 4 -6 0 6 0	01 0 -10 0 6	11 0 4 -12 0	<b>b1</b> 0 0 6 -6		$\begin{cases} -4\pi_{00} + 6\pi_{01} = 0\\ 4\pi_{00} - 6\pi_{10} + 6\pi_{11} = 0\\ 6\pi_{10} - 10\pi_{01} + 6\pi_{b1} = 0\\ 4\pi_{01} - 12\pi_{11} = 0\\ 6\pi_{11} - 6\pi_{b1} = 0 \end{cases}$ & $\pi_{00} + \pi_{10} + \pi_{01} + \pi_{11} + \pi_{b1} = 0$
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## Steady-state Distribution

i	state	$\pi_{i}$
1	00	0.3333
2	10	0.2963
3	01	0.2222
4	11	0.0741
5	b1	0.0741

## What is the average throughput of the system?

Jobs are completed at the rate **6/hr** when system is in states 3, 4, & 5,

having total probability **0.3704**.

Therefore the **throughput** is  $0.3704 \times 6/hr = 2.222/hr$ .

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