## Electric Generating

## Capacity Expansion

## A shortest-path model

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## Capacity Planning for Electric Utility

An electric utility company must schedule the addition of power generation capactiy over the next six years, given

- cumulative number of plants required each year
- fixed cost during year in which plants are constructed
- marginal cost per plant
- discount factor

The fixed cost of adding capacity in a year, independent of the number of generators added, is $1.5 \mathrm{M} \$$.
The marginal cost per generator varies by year, and is

| Year | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\$ M /$ unit | 5.4 | 5.6. | 5.8 | 5.7 | 5.5 | 5.2 |

Based upon forecasts of demand, the company has set the following goals to be achieved by the end of any year, i.e., the cumulative number of generators installed:

| Year | 1 | 2 | 3 | 4 | 5 | 6 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| \# units | 1 | 2 | 4 | 6 | 7 | 8 |

A total of eight generators will have been installed during the six-year period, then, with a restriction that no more than three may be installed during each one-year period.

In a project of this magnitude and duration, consideration of the time value of money is important. The company policy is to use a discount rate of $\mathbf{0 . 8 6 9 5 6}$, that is, the present value of a cost of $\$ 1$ incurred one year into the future is $\$ 0.86956$.


The optimal sequence of units added corresponds to a path from source node $(0,0)$, time 0,0 units added.
to the
destination node $(6,8)$, time 6,8 units added.

The cost of a link between two nodes is the cost of adding the corresponding capacity--
for example, the cost of the link

$$
(2,3) \rightarrow(3,6)
$$

is the cost of adding 3 generators in period 2 , namely

$$
1.5+3 \times 5.6=18.3
$$



Shown on the left is the shortest path from the initial node to the destination, node $(6,8)$.

The length of this shortest path (discounted for present value) is
37.7664

