

A machined part requires the following sequence of manufacturing steps:

Machine A

- Inspection A
- Machine B
- Inspection B
- Machine C
- Inspection C
- Pack & Ship

→(A) →(B**)**– ⊢→| B

During each machining step, parts could be ruined (perhaps because of a casting defect).

In the inspection step following each machine, the inspector may:

- pass the part to the next machine
- scrap the part if defective.
- return the part to the preceding machine for rework

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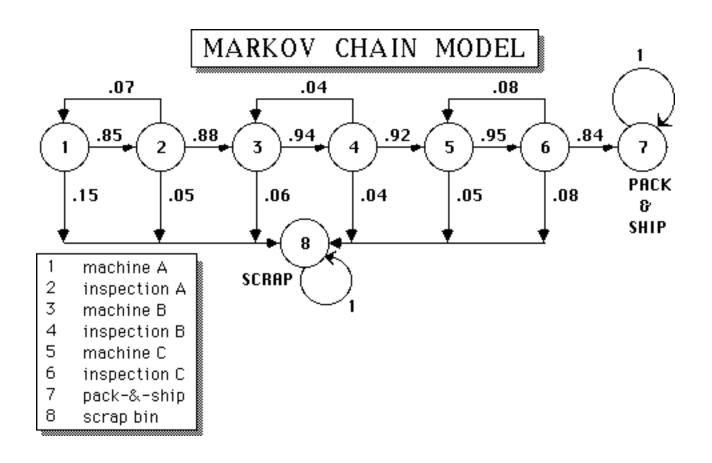
OPERATION		OPERATING COST (\$/hr.)	SCRAP RATE(%)	% SENT BACK FOR REWORK
Machine A	5.0	12.00	15	
Inspection	iA 1.6	10.00	5	7
Machine B	3.0	12.00	6	
Inspection	iB 1.6	10.00	4	4
Machine C	2.7	15.00	5	
Inspection	nC 1.6	10.00	8	8
Pack & Shi	p 0.7	5.00		

Cost of blank part: \$50

Salvage value of scrapped part: \$12

Define a stochastic process for a part:

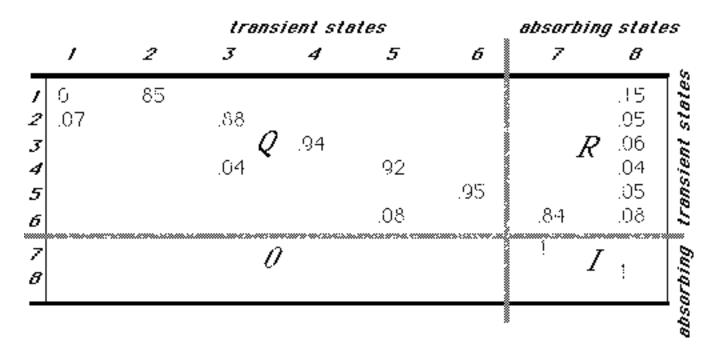
State	Location of Part
1	Machine A
2	Inspection station A
3	Machine B
4	Inspection station B
5	Machine C
6	Inspection station C
7	Pack-&-Ship Dept. 🤇
8	Pack-&-Ship Dept. Scrap bin



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		TRAN	SITION	PRO	BABILI	ΤΥ Μ	ATRIX:	
	,	2	3	4	5	6	7	8
 0 2 .0 3 4 5 6 7 8 	7	.85	.88 .04	.94	.92 .08	.95	.84 1	.15 .05 .06 .04 .05 .08

Partition the Matrix:



	F	-	transitions from transient states to transient states	Q =	0.07 0 0 0 0	0.85 0 0 0.88 0 0 0 0.04 0 0 0 0	0.94 0 0 0.92	0.95
Р	$= \begin{bmatrix} Q\\ 0 \end{bmatrix}$	R I	transitions from transient states to absorbing states	, R =	0 0 0 0.84	0.15 0.05 0.06 0.04 0.05 0.08		

EXPECTED NUMBER OF VISITS	
TO TRANSIENT STATES	

 $\mathbf{E} = (\mathbf{I} - \mathbf{Q})^{-1}$

	1	2	3	4	5	6
1:	1.06	.904	.826	.777	.773	.735
2:	.074	1.06	.972	.914	.91	.864
3:	0	0	1.04	.977	.972	.924
4:	0	0	.042	1.04	1.03	.983
5:	0	0	0	0	1.08	1.03
6:	0	0	0	0	.087	1.08
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ABSORPTION PROBABILITIES

	A =	(I	- Q)-	^{1}R
	7		8	
1: 2: 3: 4: 5: 6:	.7 .7 .8 .8	517 726 776 326 364 909	.383 .274 .224 .174 .136 .091	-
Ο.		,09	.091	_

Parts arriving at machine A have a 61.7% probability of being successfully completed!

ESTIMATED MAN-HR RQMTS PER ENTERING PART

OPERATION	STATE	MAN-HR / ENTERING PART
MACHINE A	1	5.0 × 1.06 = 5.300
INSPECTION A	2	$1.6 \times .904 = 1.446$
MACHINE B	3	3.0 × .826 = 2.478
INSPECTION B	4	$1.6 \times .777 = 1.243$
MACHINE C	5	2.7 × .773 = 2.087
INSPECTION C	6	1.6 × .735 = 1.176
PACK & SHIP	7	0.7 × .617 = 0.432
		TOTAL = 14.162 man-hrs
hrs/visit x # vi	sits	

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ESTIMATED MAN-HR RQMTS PER COMPLETED PART

Each completed part requires an expected $\frac{1}{0.617}$ i.e., 1.6207 entering parts.

So we can multiply the man-hr requirements per entering part at each stage by the factor 1.6207 to get the expected man-hr requirements per completed part.

For example, the total man-hr. requirement (for all stages) will be $14.162 \times 1.6207 = 22.95$ man-hours

ESTIMATED MAN-HR RQMTS PER COMPLETED PART

OPERATION	STATE	MAN-HR / COMPI	LETED PART
Machine A Inspection A Machine B Inspection B Machine C Inspection C	1 2 3 4 5 6	1.06 × 5 / 0.617 1.06 × 16/ 0.726 1.04 × 3 / 0.776 1.04 × 1.6/ 0.826 1.08 × 2.7/ 0.864 1.08 × 1.6/ 0.909	= 8.611 = 2.342 = 4.016 = 2.014 = 3.383 = 1.904
Pack-&-Ship	7	1 × 0.77 1.0	= 0.7

Total = 22.97 man-hrs

Expected Direct Costs per Completed Part

Materials: \$50 × 1.6207 = \$81.04

Scrap value recovered: \$12 × 1.6207 × 0.383 = \$7.45

OPERATIONS COST

OPERATION	HOURLY RATE	MAN-HRS	TOTAL COST
MACHINE A	12.00	8.613	103.40
INSPECTION A	10.00	2.343	23.43
MACHINE B	12.00	4.017	48.20
INSPECTION B	10.00	2.014	20.14
MACHINE C	15.00	3.383	50.75
INSPECTION C	10.00	1.905	19.05
PACK-&-SHIP	5.00	.700	3.50
		TOTAL =	\$ 268.40
Total Direct	<i>t Cost:</i> \$81.0	4 + \$268.40 - \$7.45	5 = \$341.99
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