

Suppose that there are 30 matches on a table. I begin by picking up 1, 2, or 3 matches. Then my opponent must pick up 1, 2, or 3 matches. We continue in this fashion until the last match is picked up, and he who picks up that last match is the loser of the game.

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What is the best strategy for playing this game?

That is, if there are x matches on the table, how many should 1 pick up?

Suppose that the loser pays \$1. Define the optimal value function

- f(x) = minimum cost if there are x matches remaining on the table, and it is your turn to remove matches.
- d(x) = optimal number of matches to remove, if x matches remain on the table.

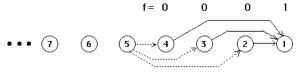
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Recursive Definition of Optimal Value Function

Assume that your opponent follows the strategy which is optimal for him. Then

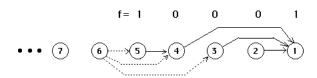
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Suppose that 5 matches remain, and it is your turn....

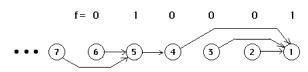
no matter whether you remove 1, 2, or 3 matches, the number remaining for you opponent will be such that his optimal cost will be 0.

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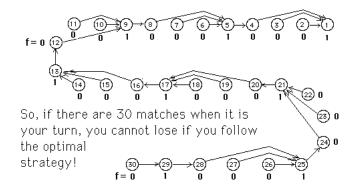


Suppose that 6 matches remain, and it is your turn... Then your cost will be

f(6) = minimum $\{1-1, 1-0, 1-0\}$ = minimum $\{0,1,1\}$ = 0 and the optimal number of matches to remove is 1 (which leaves your opponent with 5 matches on the table)



Likewise, if there are 7 matches on the table when it is your turn, you should remove 2 matches so as to leave 5 on the table when it is your opponent's turn!



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