

# Chicken Feed



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A firm manufactures **chicken feed** by mixing three different ingredients.

Each ingredient contains **four key nutrients**:

protein, fat, vitamin A, and vitamin B.

The amount of each nutrient contained in 1 kilogram of the **three basic ingredients** is:

Ingredient	Protein (grams)	Fat (grams)	Vitamin A (units)	Vitamin B (units)
1	25	11	235	12
2	45	10	160	6
3	32	7	190	10

The costs per kg of Ingredients 1, 2, and 3 are  
\$0.55, \$0.42, and \$0.38, respectively.

Each kilogram of the feed must contain

- *at least* 35 grams of protein,
- a *minimum* of 8 grams (and a *maximum* of 10 grams) of fat,
- *at least* 180 units of vitamin A and
- *at least* 9 units of vitamin B.

*Formulate an LP model for finding the feed mix that has the minimum cost per kg.*



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## Decision variables

X1 = kg. of Ingredient 1 included in mixture

X2 = kg. of Ingredient 2 included in mixture

X3 = kg. of Ingredient 3 included in mixture

# Chicken Feed

## Complete LP Formulation (LINDO)

```
MIN      0.55 X1 + 0.42 X2 + 0.38 X3
st
    25 X1 + 45 X2 + 32 X3 >= 35  ! Protein constraint
    11 X1 + 10 X2 + 7 X3 >= 8    ! Min Fat constraint
    11 X1 + 10 X2 + 7 X3 <= 10   ! Max Fat constraint
    235 X1 + 160 X2 + 190 X3 >= 180 ! Vitamin A constraint
    12 X1 + 6 X2 + 10 X3 >= 9    ! Vitamin B constraint
          X1 + X2 + X3 = 1      ! total wt of mixture

END
```

OBJECTIVE FUNCTION VALUE

1) 0.3986364

VARIABLE	VALUE	REDUCED COST
X1	0.045455	0.000000
X2	0.272727	0.000000
X3	0.681818	0.000000

ROW	SLACK OR SURPLUS	DUAL PRICES
2)	0.227273	0.000000
3)	0.000000	-0.034545
4)	2.000000	0.000000
5)	3.863636	0.000000
6)	0.000000	-0.015909
7)	0.000000	0.020909

The minimum cost mixture costs \$0.398/kg and consists of  
 0.045 kg of Ingredient 1,  
 0.273 kg of Ingredient 2 and  
 0.682 kg of Ingredient 3

*Which constraints are “tight” or “binding”?  
 Which are “loose”?*

RANGES IN WHICH THE BASIS IS UNCHANGED:

VARIABLE	CURRENT COEF	OBJ COEFFICIENT RANGES	
		ALLOWABLE INCREASE	ALLOWABLE DECREASE
X1	0.550000	INFINITY	0.116667
X2	0.420000	0.087500	0.380000
X3	0.380000	0.126667	0.350000

ROW	CURRENT RHS	RIGHTHAND SIDE RANGES	
		ALLOWABLE INCREASE	ALLOWABLE DECREASE
2	35.000000	0.227273	INFINITY
3	8.000000	2.000000	0.250000
4	10.000000	INFINITY	2.000000
5	180.000000	3.863636	INFINITY
6	9.000000	0.068493	0.333333
7	1.000000	0.017241	0.003453

## LINGO model:

```
SETS:
    INGREDIENT /1..3/: PROTEIN, FAT, VITA, VITB, COST, X;
ENDSETS

DATA:
    PROTEIN = 25 45 32;
    FAT = 11 10 7;
    VITA = 235 160 190;
    VITB = 12 6 10;
    COST = 0.55 0.42 0.38;
ENDDATA

MIN = @SUM(INGREDIENT: COST*X);
@SUM(INGREDIENT: PROTEIN * X) >= 35; ! minimum protein ;
@SUM(INGREDIENT: FAT * X) >= 8; ! minimum fat ;
@SUM(INGREDIENT: FAT * X) <= 10; ! maximum fat ;
@SUM(INGREDIENT: VITA * X) >= 180; ! minimum vitamin A ;
@SUM(INGREDIENT: VITB * X) >= 9; ! minimum vitamin B ;
@SUM(INGREDIENT: X) = 1 ; ! total weight = 1 kg;
END
```

**Chicken  
Feed**

Suppose that a new ingredient has become available with the following characteristics:

Protein	2.2%
Fat	0.9%
Vitamin A (units/kg)	200
Vitamin B (units/kg)	5
Cost (\$/kg)	\$0.36

- Modify the LINGO model in order to consider this ingredient.
- Is the solution changed?